

ACM ICPC 2016–2017  
Northeastern European Regional Contest  
Problems Review

December 4, 2016

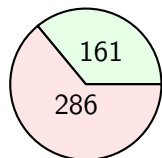
## Problems summary

- ▶ Recap: 228 teams, 13 problems, 5 hours,
- ▶ This review assumes the knowledge of the problem statements (published separately on <http://neerc.ifmo.ru/> web site)
- ▶ Summary table on the next slide lists problem name and stats
  - ▶ **author** — author of the original idea
  - ▶ **acc** — number of teams that had solved the problem (gray bar denotes a fraction of the teams that solved the problem)
  - ▶ **runs** — number of total attempts
  - ▶ **succ** — overall successful attempts rate (percent of accepted submissions to total, also shown as a bar)

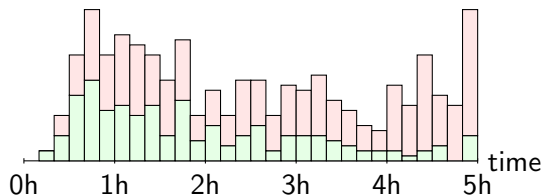
## Problems summary (2)

| <b>problem name</b>                | <b>author</b>       | <b>acc/runs</b> | <b>succ</b> |
|------------------------------------|---------------------|-----------------|-------------|
| Abbreviation                       | Roman Elizarov      | 161 / 447       | 36%         |
| Binary Code                        | Niyaz Nigmatullin   | 5 / 76          | 6%          |
| Cactus Construction                | Pavel Kunyavsky     | 8 / 20          | 40%         |
| Delight for a Cat                  | Gennady Korotkevich | 1 / 2           | 50%         |
| Expect to Wait                     | Vitaliy Aksenov     | 62 / 208        | 29%         |
| Foreign Postcards                  | Niyaz Nigmatullin   | 115 / 261       | 44%         |
| Game on Graph                      | Pavel Kunyavsky     | 3 / 12          | 25%         |
| Hard Refactoring                   | Elena Kryuchkova    | 168 / 526       | 31%         |
| Indiana Jones and the Uniform Cave | Georgiy Korneev     | 0 / 13          | 0%          |
| Jenga Boom                         | Georgiy Korneev     | 59 / 396        | 14%         |
| Kids Designing Kids                | Pavel Mavrin        | 7 / 38          | 18%         |
| List of Primes                     | Mikhail Dvorkin     | 12 / 28         | 42%         |
| Mole Tunnels                       | Borys Minaiev       | 2 / 4           | 50%         |

## Problem A. Abbreviation



Total



|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 9    | 142 | 10     | 161   |
| Rejected | 39   | 230 | 17     | 286   |
| Total    | 48   | 372 | 27     | 447   |

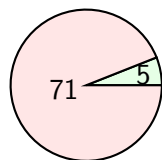
| solution         | team | att | time | size  | lang   |
|------------------|------|-----|------|-------|--------|
| <b>Fastest</b>   |      | 1   | 16   | 2,015 | C++    |
| <b>Shortest</b>  |      | 1   | 19   | 386   | Python |
| <b>Max atts.</b> |      | 9   | 292  | 4,689 | C++    |

## Problem A. Abbreviation

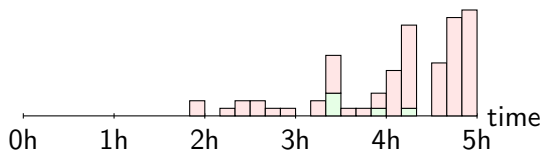
- ▶ One of the two simple problems in the contest
- ▶ Many ways to write a solution
- ▶ One of the ways is this:
  - ▶ Split each line into words and separators
  - ▶ Identify *capitalized words* per problem statement
  - ▶ Find the longest sequences of two or more words separated by a single space
  - ▶ Perform replacements per the problem statement
- ▶ The shortest solution from Ural Federal University 4 (Ankudinov, Borzunov, Stikhin) uses a single regular expression with a replacement function:

```
re.sub(r'\b[A-Z] [a-z]+( [A-Z] [a-z]+\b)+', abbr, text)
```

## Problem B. Binary Code



Total



|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 1    | 4   | 0      | 5     |
| Rejected | 1    | 70  | 0      | 71    |
| Total    | 2    | 74  | 0      | 76    |

| solution         | team | att | time | size  | lang |
|------------------|------|-----|------|-------|------|
| <b>Fastest</b>   |      | 2   | 204  | 4,918 | Java |
| <b>Shortest</b>  |      | 2   | 204  | 4,918 | Java |
| <b>Max atts.</b> |      | 5   | 205  | 4,940 | C++  |

## Problem B. Binary Code

- ▶ Solution outline: solve the problem by converting it into an instance of 2-SAT problem
  1. Build a *trie* of the given strings
  2. Define two variables  $v_i^0$  and  $v_i^1 = \bar{v}_i^1$  for each word  $s_i$  that contains a “?”
    - ▶  $v_i^0$  is *true* and  $v_i^1$  is *false* when “?” is replaced with “0” in  $s_i$
    - ▶  $v_i^0$  is *false* and  $v_i^1$  is *true* when “?” is replaced with “1” in  $s_i$
  3. Create a graph with two nodes for each string. One node for  $v_i^0$ , the other for  $v_i^1$
  4. Use the trie to convert binary code constraints into 2-SAT problem instance using *implications*
  5. Use the classical 2-SAT solution algorithm via the graph algorithm to find strongly connected components in *implications graph*

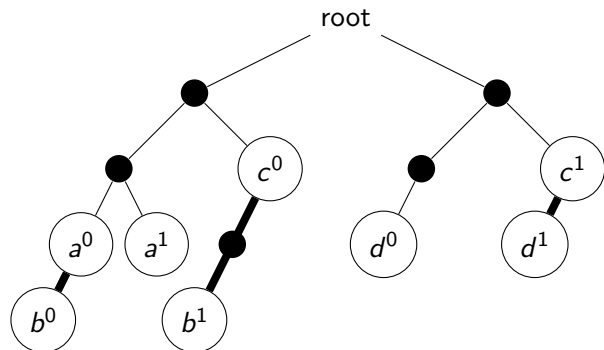
## Problem B. Binary Code — Build a trie

- ▶ Follow the classic approach, build a *binary* trie
- ▶ For strings with “?” add *both* replacements for “?” into a trie
- ▶ At the terminal nodes for the string  $s$  with “?” put the corresponding variable ( $s^0$  or  $s^1$  depending on replacement)
- ▶ At the terminal nodes for the string  $s$  *without* “?” put the separate variable  $T$  that is always *true*
  - ▶ If more than one string without “?” ends at the same node of the trie, the answer is “NO”



## Problem B. Binary Code — Trie example

- ▶ Trie for the first example



a: 00?  
b: 0?00  
c: ?1  
d: 1?0

### Implications

$a^0$  nand  $b^0$ :

$$a^0 \rightarrow b^1$$

$$b^0 \rightarrow a^1$$

$c^0$  nand  $b^1$ :

$$c^0 \rightarrow b^0$$

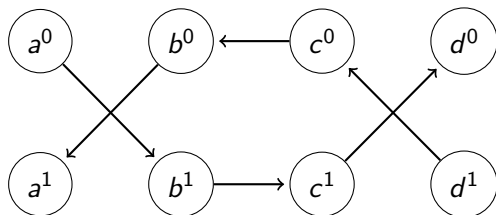
$$b^1 \rightarrow c^1$$

$c^1$  nand  $d^1$ :

$$c^1 \rightarrow d^0$$

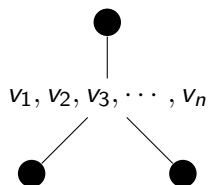
$$d^1 \rightarrow c^0$$

## Problem B. Binary Code — Implications graph example



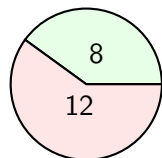
- ▶ Classic 2-SAT algorithm finds the answer or decides that it is impossible
- ▶ The sample output assigns *true* to  $a^0$ ,  $b^1$ ,  $c^1$ ,  $d^0$

## Problem B. Binary Code — Many terminals at node

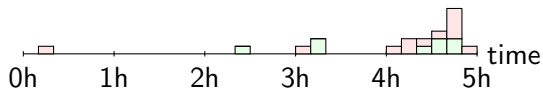


- ▶ Node in a trie can have many terminals (variables) at one node
- ▶ At most one of them can be present in a binary code
- ▶ We can express this constraint in  $O(n)$  implications using  $n$  additional variable pairs
  - ▶ Define additional variable  $r_i$  to be *true* if and only if at least one  $v_j, j \geq i$  is *true*
- ▶ Or exclude all  $v_i$  and  $v_j$  pairs, but return “NO” answer when  $n$  is more than the depth of this node in a trie plus one

## Problem C. Cactus Construction



Total

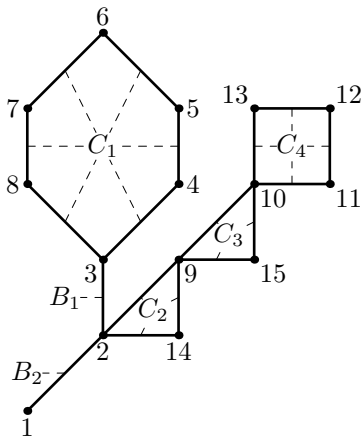


|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 0    | 8   | 0      | 8     |
| Rejected | 0    | 12  | 0      | 12    |
| Total    | 0    | 20  | 0      | 20    |

| solution         | team | att | time | size  | lang |
|------------------|------|-----|------|-------|------|
| <b>Fastest</b>   |      | 1   | 142  | 4,953 | C++  |
| <b>Shortest</b>  |      | 1   | 261  | 2,512 | C++  |
| <b>Max atts.</b> |      | 4   | 275  | 6,786 | C++  |

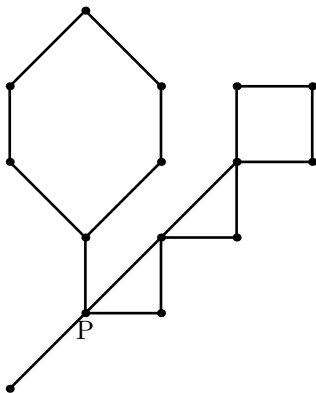
## Problem C. Cactus Construction (1)

- ▶ Depth-first search (DFS) of the cactus to split the edges of the cactus into disjoint sets of *bridges*  $B_i$  and *cycles*  $C_i$ 
  - ▶ Each back edge found during DFS signals a cycle
  - ▶ All edges that do not belong to any cycle are bridges



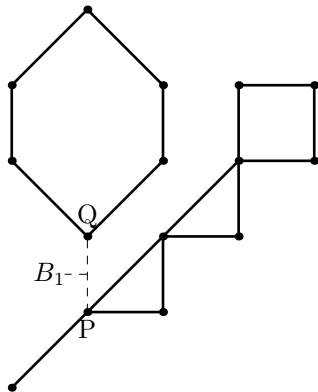
## Problem C. Cactus Construction (2)

- ▶ Recursive procedure: given a cactus and a vertex  $P$  in it, construct the cactus in such a way that all vertices have color 2 except  $P$ , which must have color 1.
- ▶ Pick any vertex as  $P$  to start the procedure.



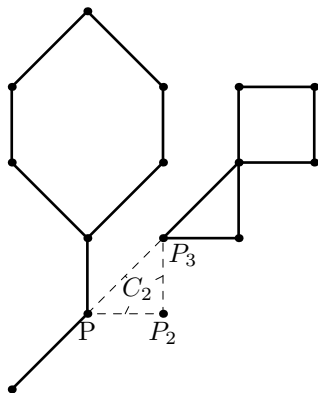
## Problem C. Cactus Construction (3)

- ▶ If there's a bridge  $B_i$  connecting  $P$  with some other vertex  $Q$ :
  - ▶ Remove the bridge  $B_i$ .
  - ▶ Recursively construct two halves using  $P$  and  $Q$  as designated vertices (color 1).
  - ▶ Build edge  $B_i$  and color  $Q$  with 2 (more details later).



## Problem C. Cactus Construction (4)

- ▶ If there's a cycle  $C_i$  passing through  $P = P_1, P_2, \dots, P_k$ :
  - ▶ Remove all edges of  $C_i$ .
  - ▶ Graph splits into  $k$  components. Recursively construct them using  $P_j$  as designated vertices (color 1).
  - ▶ Build all edges of  $C_i$  and color  $P_2, P_3, \dots, P_k$  with 2 (more details later).





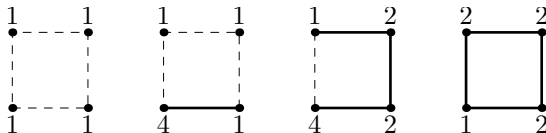
## Problem C. Cactus Construction (5)

- ▶ How to build a new bridge connecting two components with designated vertices  $P$  and  $Q$ :
  - ▶ Initially  $P$  and  $Q$  are colored with 1, the rest with 2.
  - ▶ Recolor 1 to 3 in the component of  $Q$ .
  - ▶ Join components of  $P$  and  $Q$ .
  - ▶ Connect colors 1 and 3, connecting  $P$  and  $Q$ .
  - ▶ Recolor 3 to 2.

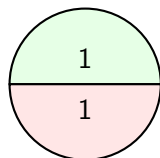


## Problem C. Cactus Construction (6)

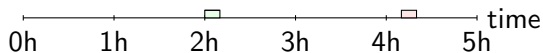
- ▶ How to build a new cycle connecting  $k$  components with designated vertices  $P = P_1, P_2, \dots, P_k$ :
  - ▶ Build edges of the cycle one by one, starting with the edge between  $P_1$  and  $P_2$ .
  - ▶ Each edge except the last one is built as a new bridge.
  - ▶ But remember to recolor the first vertex  $P_1$  to 4 instead of 2 after building the first edge.
  - ▶ This allows to close the cycle in the end by connecting colors 1 and 4.



## Problem D. Delight for a Cat



Total



|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 0    | 1   | 0      | 1     |
| Rejected | 0    | 1   | 0      | 1     |
| Total    | 0    | 2   | 0      | 2     |

| solution         | team | att | time | size  | lang |
|------------------|------|-----|------|-------|------|
| <b>Fastest</b>   |      | 1   | 123  | 2,825 | C++  |
| <b>Shortest</b>  |      | 1   | 123  | 2,825 | C++  |
| <b>Max atts.</b> |      | 1   | 123  | 2,825 | C++  |

## Problem D. Delight for a Cat

- ▶ Out of every  $k$  consecutive hours, the cat must sleep at least  $min_s$  hours and eat at least  $min_e$  hours
  - ▶ Let  $max_e = k - min_s$ , now the cat must eat between  $min_e$  and  $max_e$  hours out of every  $k$
- ▶ Let's say that the cat is sleeping by default, and it gets  $\delta_i = e_i - s_i$  delight for eating at hour  $i$ 
  - ▶ In the end, add  $\sum_{i=1}^n s_i$  to the answer

## Problem D. Delight for a Cat (2)

- ▶ Let  $\min_e = 0$ ,  $\max_e = 1$
- ▶ Dynamic programming:
  - ▶ Let  $f_i$  be the maximum amount of delight for hours from  $i$  to  $n$
  - ▶  $f_i = \max(f_{i+1}, \delta_i + f_{i+k})$
  - ▶ Here, we define  $f_i = 0$  for  $i > n$
- ▶ Dynamic programming  $\rightarrow$  shortest path:
  - ▶ Vertices  $S$ ,  $T$  and  $1, 2, \dots, n$
  - ▶ Edge from vertex  $i$  to vertex  $i + 1$  (or  $T$ , if  $i + 1 > n$ ) with cost 0
  - ▶ Edge from vertex  $i$  to vertex  $i + k$  (or  $T$ , if  $i + k > n$ ) with cost  $-\delta_i$
  - ▶ Edges from vertex  $S$  to vertices  $1, 2, \dots, k$  with cost 0
  - ▶ Negated length of the shortest path from  $S$  to  $T$  is the answer

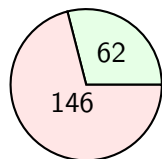
## Problem D. Delight for a Cat (3)

- ▶ Let  $\min_e = 0$ ,  $\max_e \geq 0$
- ▶ Graph for  $\max_e = 1 \rightarrow$  network for  $\max_e \geq 0$ :
  - ▶ Vertices  $S$ ,  $T$  and  $1, 2, \dots, n$
  - ▶ Edge from vertex  $i$  to vertex  $i + 1$  (or  $T$ , if  $i + 1 > n$ ) with cost 0 and capacity  $\max_e$
  - ▶ Edge from vertex  $i$  to vertex  $i + k$  (or  $T$ , if  $i + k > n$ ) with cost  $-\delta_i$  and capacity 1
  - ▶ Edges from vertex  $S$  to vertices  $1, 2, \dots, k$  with cost 0 and capacity  $\infty$
  - ▶ Negated minimum cost of flow of value  $\max_e$  from  $S$  to  $T$  is the answer

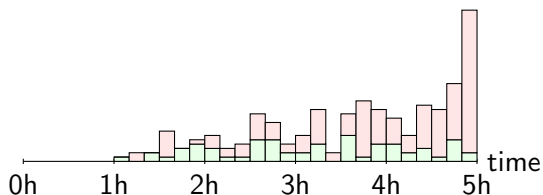
## Problem D. Delight for a Cat (4)

- ▶ Let  $max_e \geq min_e \geq 0$
- ▶ Network for  $min_e = 0 \rightarrow$  network for  $min_e \geq 0$ :
  - ▶ Vertices  $S, T$  and  $1, 2, \dots, n$
  - ▶ Edge from vertex  $i$  to vertex  $i + 1$  (or  $T$ , if  $i + 1 > n$ ) with cost 0 and capacity  $max_e - min_e$
  - ▶ Edge from vertex  $i$  to vertex  $i + k$  (or  $T$ , if  $i + k > n$ ) with cost  $-\delta_i$  and capacity 1
  - ▶ Edges from vertex  $S$  to vertices  $1, 2, \dots, k$  with cost 0 and capacity  $\infty$
  - ▶ Negated minimum cost of flow of value  $max_e$  from  $S$  to  $T$  is the answer

## Problem E. Expect to Wait



Total

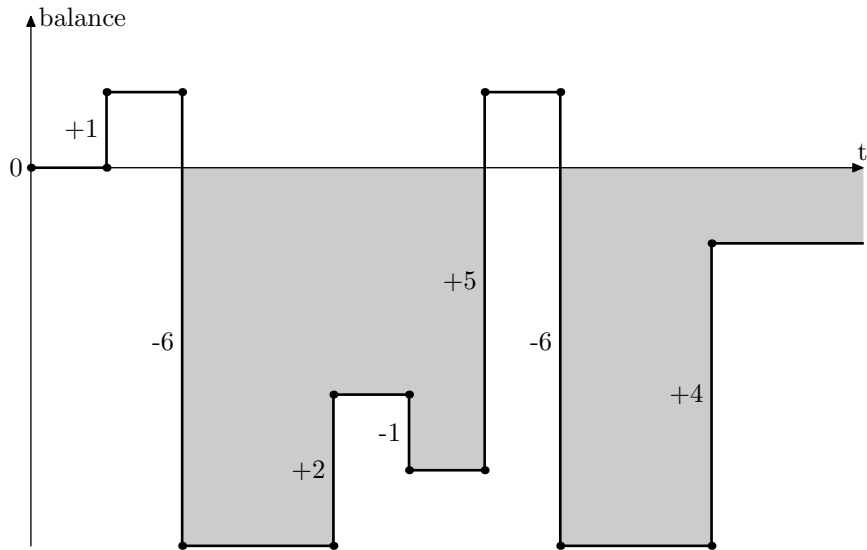


|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 3    | 59  | 0      | 62    |
| Rejected | 3    | 143 | 0      | 146   |
| Total    | 6    | 202 | 0      | 208   |

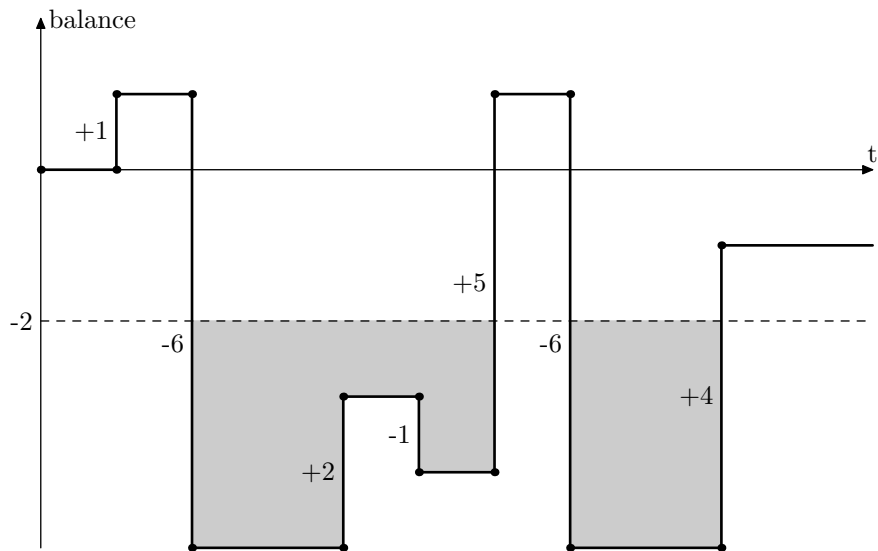
| solution         | team | att | time | size  | lang |
|------------------|------|-----|------|-------|------|
| <b>Fastest</b>   |      | 1   | 61   | 2,093 | C++  |
| <b>Shortest</b>  |      | 1   | 115  | 1,274 | C++  |
| <b>Max atts.</b> |      | 6   | 285  | 2,167 | C++  |



## Problem E. Expect to Wait



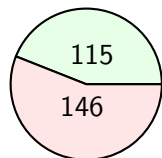
## Problem E. Expect to Wait (2)



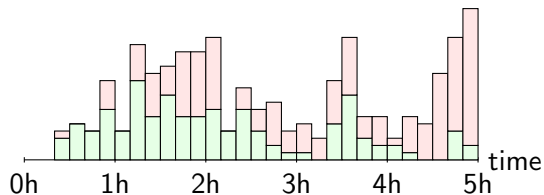
## Problem E. Expect to Wait (3)

- ▶ For  $b_i$ , calculate square under line  $balance = -b_i$
- ▶ Scan-line
- ▶  $O(N \log N + Q \log Q)$

## Problem F. Foreign Postcards



Total



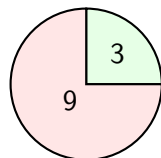
|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 3    | 112 | 0      | 115   |
| Rejected | 17   | 126 | 3      | 146   |
| Total    | 20   | 238 | 3      | 261   |

| solution         | team | att | time | size  | lang |
|------------------|------|-----|------|-------|------|
| <b>Fastest</b>   |      | 1   | 23   | 1,774 | C++  |
| <b>Shortest</b>  |      | 1   | 68   | 483   | C++  |
| <b>Max atts.</b> |      | 15  | 281  | 1,030 | C++  |

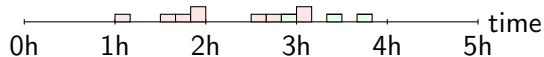
## Problem F. Foreign Postcards

- ▶  $A_i$  is the expected number of W's starting from position  $i$ .
- ▶  $A_i = \frac{1}{n-i} \sum_{j=i+1}^n A_j + |\{k \mid k \in [i, j) \wedge S_i \neq S_k\}|$
- ▶ Straightforward calculation —  $O(N^2)$  solution.
- ▶ The second sum is  $\sum_{j=i+1}^n [S_i \neq S_j] \cdot (n - j)$
- ▶ It is equal to either  $\sum_{S_j=C} (n - j)$  or  $\sum_{S_j=W} (n - j)$
- ▶ Calculate everything in linear time,  $O(N)$  solution.

## Problem G. Game on Graph



Total



|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 0    | 3   | 0      | 3     |
| Rejected | 0    | 9   | 0      | 9     |
| Total    | 0    | 12  | 0      | 12    |

| solution         | team | att | time | size  | lang |
|------------------|------|-----|------|-------|------|
| <b>Fastest</b>   |      | 7   | 174  | 3,103 | C++  |
| <b>Shortest</b>  |      | 2   | 221  | 2,023 | C++  |
| <b>Max atts.</b> |      | 7   | 174  | 3,103 | C++  |

## Problem G. Game on Graph

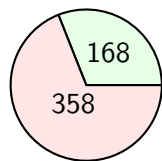
- ▶ Let's name a pair of vertex and player who has move now a *position* in game.
- ▶ If first player can enforce draw, regardless of second player moves, he will do it.
- ▶ If second player can enforce his winning, regardless of first player moves, he will do it.
- ▶ If first player can't enforce draw, second player will not allow draw happen, because it's worst result for him
- ▶ If second player can't enforce winning, first player will not allow him to win, because it's worst result for him.
- ▶ So, in all other positions, first player will win.

## Problem G. Game on Graph (2)

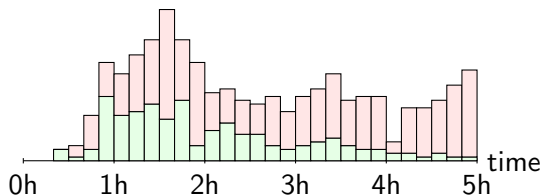
- ▶ How to find all positions, where first player can enforce draw?
- ▶ Let's put in queue all positions, where player have no moves.
- ▶ While queue is not empty, get next position from queue.
- ▶ If it's first player turn, than mark all positions of second player with move to this position and put them to queue.
- ▶ If it's second player turn, than mark all positions of first player, where it's last move to non-marked positions, and put them to queue.
- ▶ First player can enforce draw, iff position is not marked.
- ▶ Postions, where second player can enforce win, can be found in similar way.



## Problem H. Hard Refactoring



Total



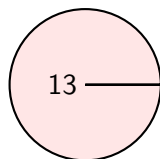
|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 10   | 154 | 4      | 168   |
| Rejected | 29   | 318 | 11     | 358   |
| Total    | 39   | 472 | 15     | 526   |

| solution         | team | att | time | size  | lang   |
|------------------|------|-----|------|-------|--------|
| <b>Fastest</b>   |      | 1   | 20   | 1,982 | C++    |
| <b>Shortest</b>  |      | 2   | 109  | 1,303 | Python |
| <b>Max atts.</b> |      | 11  | 242  | 2,721 | C++    |

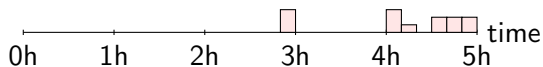
## Problem H. Hard Refactoring

- ▶ It is an easy problem. The hardest part is parsing
- ▶ Once input is parsed, it is Ok to simply fill a Boolean array of  $2^{16}$  items, then print the answer
- ▶ The only tricky thing in this problem are the edges of the set of 16-bit integers and the corresponding samples are given in the problem statement

## Problem I. Indiana Jones and the Uniform Cave



Total



|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 0    | 0   | 0      | 0     |
| Rejected | 0    | 13  | 0      | 13    |
| Total    | 0    | 13  | 0      | 13    |

## Problem I. Indiana Jones and the Uniform Cave

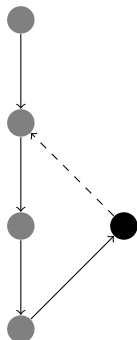
- ▶ Solution overview: use depth-first-search (DFS) to recursively traverse the graph
  - ▶ Mark with “right” chambers on the current DFS path to root. Let us call them *gray* chambers
  - ▶ Mark with “left” chambers that were already visited. Let us call them *black* chambers
- ▶ At each node do “1 right 1”  $m$  times to check all outgoing passages
- ▶ Keep the track of the highest gray (“right”) chamber encountered down from the current chamber in dfs and the number of the corresponding passage in the chamber
- ▶ When all  $m$  passages out of the chamber are visited, follow to that chamber until gray (“right”) chamber is encountered and follow down to the previous chamber

## Problem I. Indiana Jones and the Uniform Cave (2)



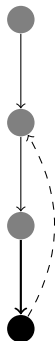
- ▶ When gray (“right”) chamber is encountered:
- ▶ Mark it with “left”
- ▶ Follow gray (“right”) chambers with “0 right 0” until the chamber previously marked with “left” is reached
- ▶ Count the number of passages visited
- ▶ Make another pass, taking one fewer passage to “backtrack” and put stones at “right” again
- ▶ Remember how many gray chambers up the path we’ve got to!

## Problem I. Indiana Jones and the Uniform Cave (3)



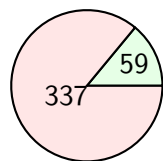
- ▶ When black (“left”) chamber is encountered:
- ▶ Follow black (“left”) chambers with “0 left 0”
- ▶ Follow gray (“right”) chambers with “0 right 0”
- ▶ Count the number of passages visited
- ▶ Make another pass, taking one fewer passage to “backtrack”
- ▶ Put stones at “right” or “left” as they were
- ▶ Remember how many gray chambers up the path we’ve got to!

## Problem I. Indiana Jones and the Uniform Cave (4)

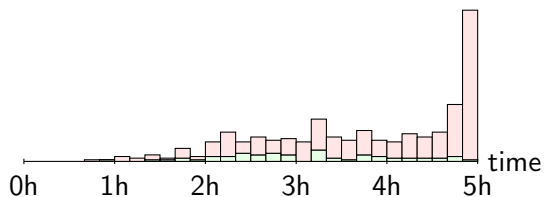


- ▶ When leaving the chamber in dfs (after visiting all  $m$  passages), use the passage that is leading to the highest gray chamber
- ▶ Stones were properly left in place previously, just follow them
- ▶ Mark the chamber we are leaving as black (“left”)

## Problem J. Jenga Boom



Total



|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 2    | 57  | 0      | 59    |
| Rejected | 21   | 316 | 0      | 337   |
| Total    | 23   | 373 | 0      | 396   |

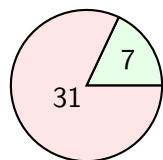
| solution         | team | att | time | size  | lang |
|------------------|------|-----|------|-------|------|
| <b>Fastest</b>   |      | 1   | 55   | 1,919 | C++  |
| <b>Shortest</b>  |      | 1   | 138  | 1,707 | C++  |
| <b>Max atts.</b> |      | 14  | 198  | 2,669 | C++  |



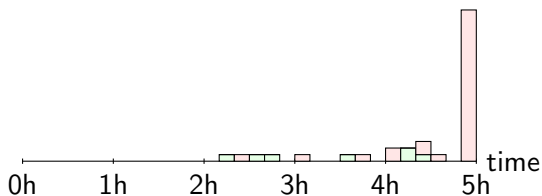
## Problem J. Jenga Boom

- ▶ The solution is straightforward
- ▶ Keep the sum of coordinates of centers of remaining blocks at each level
- ▶ Keep the set of remaining blocks (in a Boolean array)
- ▶ When a block is removed, update this information, then recheck stability condition for every level (top to bottom)
  - ▶ Sum centers of masses and count total number of blocks above the current cross-section
  - ▶ Use the set of remaining block at the level immediately below the current cross-section to compute its convex hull in a trivial way
- ▶ Some tips
  - ▶ The number  $w$  is irrelevant to the problem
  - ▶ It is easier to compute everything in 64-bit integer numbers
  - ▶ Do not do binary search on answer! Simulate every block removal

## Problem K. Kids Designing Kids



Total



|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 0    | 7   | 0      | 7     |
| Rejected | 3    | 28  | 0      | 31    |
| Total    | 3    | 35  | 0      | 38    |

| solution         | team | att | time | size  | lang |
|------------------|------|-----|------|-------|------|
| <b>Fastest</b>   |      | 1   | 133  | 3,236 | C++  |
| <b>Shortest</b>  |      | 1   | 258  | 2,613 | C++  |
| <b>Max atts.</b> |      | 4   | 252  | 3,682 | C++  |

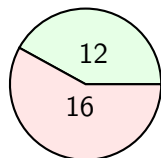
## Problem K. Kids Designing Kids

- ▶ Find the top-left freckle in each of three given pictures.
- ▶ We'll prove that after moving the figures, some two of these three freckles must be in the same point.
- ▶ There are only three possible shifts, check them all.
- ▶ To check if two pictures are the same, again find top-left freckles in each of them. These freckles must be in the same point.

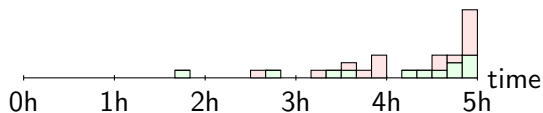
## Problem K. Kids Designing Kids — Proof

- ▶ Problem is equal to the following: move figures  $A$ ,  $B$  and  $C$  in such a way that  $A \oplus B \oplus C = \emptyset$  (empty figure).
- ▶ Let's look on top-left freckle in each picture. Suppose that after moving, they are in different points.
- ▶ Now let's find the top-left freckle from these three.
- ▶ This freckle will be present in the final symmetrical difference  $A \oplus B \oplus C$ , because it cannot be denied by any other freckle.

## Problem L. List of Primes



Total



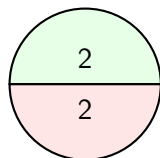
|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 0    | 12  | 0      | 12    |
| Rejected | 0    | 16  | 0      | 16    |
| Total    | 0    | 28  | 0      | 28    |

| solution         | team | att | time | size  | lang |
|------------------|------|-----|------|-------|------|
| <b>Fastest</b>   |      | 1   | 108  | 3,093 | C++  |
| <b>Shortest</b>  |      | 1   | 108  | 3,093 | C++  |
| <b>Max atts.</b> |      | 4   | 294  | 4,471 | C++  |

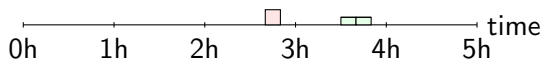
## Problem L. List of Primes

- ▶ Recursive procedure — output all sets with the following properties:
  - ▶ from the first  $x$  primes the set  $prefix$  is selected;
  - ▶ all the other selected primes add up to  $sum$ .
- ▶  $output(x, prefix, sum)$ 
  - ▶  $output(x + 1, prefix + [p_{x+1}], sum - p_{x+1})$
  - ▶  $output(x + 1, prefix, sum)$
- ▶ If the output is to left from the desired segment, skip it without going deeper in recursion.
- ▶ Precalculte number and total length of all sets in which:
  - ▶ the first  $x$  primes are not used;
  - ▶ selected primes add up to  $sum$ .
- ▶ Run  $output(0, [], sum)$  for  $sum = 2, 3, 4, \dots$

## Problem M. Mole Tunnels



Total

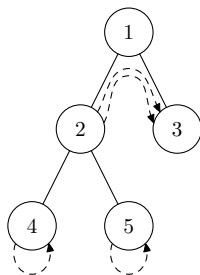


|          | Java | C++ | Python | Total |
|----------|------|-----|--------|-------|
| Accepted | 0    | 2   | 0      | 2     |
| Rejected | 0    | 2   | 0      | 2     |
| Total    | 0    | 4   | 0      | 4     |

| solution         | team | att | time | size  | lang |
|------------------|------|-----|------|-------|------|
| <b>Fastest</b>   |      | 3   | 215  | 3,397 | C++  |
| <b>Shortest</b>  |      | 1   | 227  | 2,185 | C++  |
| <b>Max atts.</b> |      | 3   | 215  | 3,397 | C++  |

## Problem M. Mole Tunnels

- ▶ Cannot be solved with Minimum Cost Maximum Flow algorithm (too slow)
- ▶ We need to find shortest path in a faster way
- ▶ Calculate dynamic programming: shortest path in a subtree of vertex  $v$
- ▶ Iterate over all possible LCA to find next shortest path
- ▶ After sending flow along augmenting path dynamic programming values changes only for at most 40 vertices





# Credits

- ▶ Special thanks to all jury members and assistants (in alphabetic order):

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