

Merging Amulets

To solve this problem, we will use the fact that gcd changes at most $\log A$ times, where A is the maximum value among a_i . We will find the prefix and suffix gcd , denoting them as p_i and s_i , respectively.

We will divide the calculation of the final sum of gcd into 3 stages:

1. The segment $[1, n]$, to find the answer we need to calculate the lcm of the entire array. This can be done using the Sieve of Eratosthenes and prime factorization of each element;
2. Segments $[i, j]$ such that $p_i = p_{i+1}$ and $s_{j-1} = s_j$. The answer for such segments will be $\text{gcd}(p_i, s_j)$, since lcm will definitely be divisible by $\text{gcd}(p_i, s_j)$, and the final gcd cannot exceed this value. Such segments can be counted quickly if we know in advance the positions where p_i and s_j change;
3. The remaining segments, specifically those $[i, j]$ such that $p_i \neq p_{i+1}$ or $s_{j-1} \neq s_j$, since gcd changes at most $\log A$ times, there will be at most $O(n \log n)$ such segments. Therefore, they can be counted with a straightforward pass through the array.

The final answer will consist of the sum of all three types of segments.