

- 12.1. The mage has n spells and m mana points. The i -th spell needs c_i mana points and deals d_i damage to the enemy. Kill a monster with h health points using as little mana as possible. Time $O(nm)$.
- 12.2. Team of Peter and Paul won n prizes in a programming contest, with a total value of r . They want to divide them among themselves so that the difference in total cost is minimal. Time $O(nr)$.
- 12.3. The same task, but time $O(n \cdot 2^{n/2})$.
- 12.4. Team of Peter and Paul again won $n = 2k$ prizes with a total value of r . They want to divide them among themselves so that everyone gets k prizes, and the difference in total cost is minimal. Time $O(n^2r)$.
- 12.5. The same task, but time $O(n \cdot 2^{n/2})$.
- 12.6. Peter and Paul called their friend Mary and they won another contest, they got n prizes with a total value of r . They want to divide them so that the difference between the maximum and minimum shares is minimal. Time $O(nr^2)$.
- 12.7. Given a graph, paint its vertices in the minimum number of colors so that each edge connects vertices of different colors. Time $O(3^n)$.
- 12.8. Peter solves the knapsack problem without costs (you need to find the maximum total weight no more than S) with a greedy algorithm, it works like this. Let some items have already been taken, and their total weight is equal to T , then at the next step of the algorithm Peter will take the item with the maximum weight among those for which $T + w_i \leq S$. If there are none, then the algorithm terminates. Let this algorithm get a set with the sum ANS , and the optimal answer is OPT . On which test will the ANS/OPT ratio be minimal?