

- 14.1. Let the number of possible keys be $U > nm$, where n is the number of elements in the hash table, and m is its size. Show that for any hash function, in the worst case, it is possible for all n elements to fall into same bucket of the hash table.
- 14.2. Let $h(k)$ be a random hash function. What is the mathematical expectation of the number of collisions (the number of pairs $(x, y), x \neq y$ such that $h(x) = h(y)$)?
- 14.3. We will resolve collisions using lists, but keep the lists in sorted order. How does this affect the worst case and average time complexity?
- 14.4. Add to the hash table the ability to iterate all its elements in the order in which they were added in $O(n)$.
- 14.5. Add the `merge` operation to the hash set, which combines two sets into one. Amortized running time $O(\log n)$.
- 14.6. See how the `Long.hashCode()` method works in Java. How can you generate many `Long`s with the same hash? Try to put them in `HashSet<Long>` and then put in another `HashSet <Long>` the same number of random `Long`s, look at how much runtime differs.
- 14.7. The same with `String.hashCode()`.
- 14.8. Add a `countUnique` operation to the dequeue, which returns the number of distinct items in the queue. Time $O(1)$.