

- 9.1. How many vertices of rank r are there in a binomial tree of rank k ?
- 9.2. Develop a binomial heap merging algorithm that goes from large trees to smaller ones, with the same time complexity.
- 9.3. One item is added to the binomial heap of size n . How to quickly figure out how many binomial tree merges will happen?
- 9.4. Show that the amortized cost of the `insert` operation in binomial heap is $O(1)$ (assuming the amortized cost of the remaining operations is $O(\log n)$).
- 9.5. How can the binomial heap be modified so that `insert` runs in true $O(1)$? (google the Knuth counter)
- 9.6. Add a key increment operation to the binomial heap, in $O(\log n)$. Is it possible to make the key increment operation faster than $O(\log n)$?
- 9.7. Prove that the maximum rank of a tree in the Fibonacci heap is $O(\log n)$.
- 9.8. Show that for any n there is a sequence of operations that results in the Fibonacci heap containing a tree that is a chain of n elements.