

## Problem A. A+B

Input file: `aplusb.in`  
Output file: `aplusb.out`  
Time limit: 2 seconds  
Memory limit: 64 megabytes

The *Research Institute of Given Strings (RIGS)* is a well-known place where people investigate anything about strings. Peter works in the department of string operations of *RIGS*. His department invents different ways to add, multiply, divide strings and even to take a logarithm of a string based on another one.

Now Peter is involved in the new project concerning orthogonal strings. Peter proposed that two strings  $P = P_1P_2 \dots P_n$  and  $Q = Q_1Q_2 \dots Q_n$  of equal length  $n$  are called *orthogonal*, if  $P_i \neq Q_i$  for each  $i$  in the range  $1..n$ . String  $S$  of length  $n$  is called orthogonal to set of strings  $V = \{V_1, V_2, \dots, V_m\}$  (each of length  $n$  too) if  $S$  is orthogonal to  $V_j$  for any  $j$  in range  $1..m$ .

Peter's task is to invent the operation of *orthogonal sum* of two given strings. The current Peter's proposal allows to add only strings on a basis of some set, if they are orthogonal to this set. To do this, Peter selects an arbitrary set of strings  $V$  such that all strings in  $V$  have the same length  $n$ . Then Peter takes all strings of length  $n$  orthogonal to  $V$  over a fixed alphabet and sorts them, thus obtaining a sorted sequence of strings  $T$ . Let's denote the length of sequence  $T$  as  $M$ , and enumerate the elements of this sequence as  $T_0, T_1, \dots, T_{M-1}$ . Now Peter says that the orthogonal sum of two strings  $A = T_a$  and  $B = T_b$  is a string  $C = T_c$  where  $c = (a + b) \bmod M$ .

Your task is to find the orthogonal sum of two given strings  $A$  and  $B$  on the basis of a given set  $V$  over the alphabet of small English letters.

### Input

The first line of the input file contains two integers:  $n$  — the length of each string ( $1 \leq n \leq 100\,000$ ) and  $k$  — the cardinality of  $V$  ( $1 \leq n \cdot k \leq 100\,000$ ). The next  $k$  lines contains strings  $V_1, V_2, \dots, V_k$ .

The last two lines contain strings  $A$  and  $B$  of length  $n$ . All strings  $V_j, A$  and  $B$  consist of small letters of English alphabet. It is guaranteed that  $A$  and  $B$  are orthogonal to  $V$ .

### Output

Output the orthogonal sum of strings  $A$  and  $B$  on the basis  $V$ .

### Example

<code>aplusb.in</code>	<code>aplusb.out</code>
2 2 ac ad bb bb	be
2 1 yy zz zz	zx

## Problem B. Beer Refrigerator

Input file: `beer.in`  
Output file: `beer.out`  
Time limit: 2 seconds  
Memory limit: 64 megabytes

*Beer Lovers Club* makes regular parties. They hate warm beer, but club's refrigerator is too small to store enough beer for the whole company. So they decided to order a special super-big beer refrigerator. The new refrigerator should be a parallelepiped  $a \times b \times c$  and store exactly  $n$  cubical  $1 \times 1 \times 1$  beer boxes (the club has  $n$  members). To decrease losses of cold, the total area of the surface of the refrigerator must be as small as possible.

For example, if the capacity of the refrigerator must be 12, the possible variants are:

Dimensions	Surface Area
$3 \times 2 \times 2$	32
$4 \times 3 \times 1$	38
$6 \times 2 \times 1$	40
$12 \times 1 \times 1$	50

The best variant in this case is  $3 \times 2 \times 2$ .

Help the beer lovers to find the optimal dimensions for their new refrigerator.

### Input

The input file contains single integer number  $n$  ( $1 \leq n \leq 10^6$ ) — the capacity of the refrigerator.

### Output

Output three integer numbers:  $a$ ,  $b$  and  $c$  — the optimal dimensions of the refrigerator. If there are several solutions, output any of them.

### Example

<code>beer.in</code>	<code>beer.out</code>
12	3 2 2
13	1 13 1
1000000	100 100 100

## Problem C. Crosses and Crosses

Input file:            `crosses.in`  
Output file:         `crosses.out`  
Time limit:          2 seconds  
Memory limit:       64 megabytes

The game of *Crosses and Crosses* is played on the field of  $1 \times n$  cells. Two players make moves in turn. Each move the player selects any free cell on the field and puts a cross '×' to it. If after the player's move there are three crosses in a row, he wins.

You are given  $n$ . Find out who wins if both players play optimally.

### Input

Input file contains one integer number  $n$  ( $3 \leq n \leq 2000$ ).

### Output

Output '1' if the first player wins, or '2' if the second player does.

### Example

<code>crosses.in</code>	<code>crosses.out</code>
3	1
6	2

## Problem D. Domestic Networks

Input file:            domestic.in  
Output file:           domestic.out  
Time limit:            2 seconds  
Memory limit:         64 megabytes

Alex is a system administrator of *Domestic Networks Inc.* His network connects apartments and spans over multiple buildings.

The network expands and Alex has to design a new network segment. He has a map that shows apartments to connect and possible links. Each link connects two apartments and for each possible link its length is known. The goal is to make all apartments connected (possibly through other apartments).

*Domestic Networks Inc.* buys cable in the nearest cable shop. Unfortunately, shop sells only category 5 and 6 cables at price of  $p_5$  and  $p_6$  rubles per meter respectively. Moreover, there are only  $q_5$  meters of category 5 cable and  $q_6$  meters of category 6 cable available in the shop.

Help Alex to solve a hard problem: make a new network construction plan with possible minimal cost. A plan consists of list of links to be made and cable category for each link (each link should be a single piece of cable of either 5 or 6 category). The cost of the plan is the sum of cost of all cables. The total length of cables of each category used in the plan should not exceed the quantity of the cable available in the shop.

### Input

The first line of the input file contains two numbers:  $n$  — the number of apartments to be connected and  $m$  — the number of possible links ( $1 \leq n \leq 1000$ ,  $1 \leq m \leq 10\,000$ ).

Following  $m$  lines contain possible link descriptions. Each description consists of three integer numbers:  $a_i$  — apartments that can be connected by the link and  $l_i$  — link length in meters ( $0 \leq l_i \leq 100$ ). Apartments are numbered from 1 to  $n$ .

The last line of the input file contains four integer numbers:  $p_5$ ,  $q_5$ ,  $p_6$  and  $q_6$  — price and quantity of category 5 and 6 cables respectively ( $1 \leq p_i, q_i \leq 10\,000$ ).

### Output

If all apartments can be connected with the available cable, output  $n$  lines — an optimal network construction plan. The first line of the plan must contain plan's cost. Other lines of the plan must consist of two integer numbers each:  $a_i$  and  $c_i$  — number of the link to make and  $c_i$  — the category of the cable to make it of. Links are numbered from 1 to  $m$  in the order they are specified in the input file. If there are more than one optimal plans, output any of them.

If there is no plan meeting all requirements, output a single word "Impossible".

### Example

domestic.in	domestic.out
6 7	65
1 2 7	1 5
2 6 5	2 6
1 4 8	4 6
2 3 5	5 6
3 4 5	7 5
5 6 6	
3 5 3	
2 11 3 100	

## Problem E. Elevator

Input file: `elevator.in`  
Output file: `elevator.out`  
Time limit: 2 seconds  
Memory limit: 64 megabytes

Edward works as an engineer for *Non-trivial Elevators: Engineering, Research and Construction (NEERC)*. His new task is to design a brand new elevator for a skyscraper with  $h$  floors.

Edward has an idée fixe: he thinks that four buttons are enough to control the movement of the elevator. His last proposal suggests the following four buttons:

- Move  $a$  floors up.
- Move  $b$  floors up.
- Move  $c$  floors up.
- Return to the first floor.

Initially, the elevator is on the first floor. A passenger uses the first three buttons to reach the floor she needs. If a passenger tries to move  $a$ ,  $b$  or  $c$  floors up and there is no such floor (she attempts to move higher than the  $h$ -th floor), the elevator doesn't move.

To prove his plan worthy, Edward wants to know how many floors are actually accessible from the first floor via his elevator. Help him calculate this number.

### Input

The first line of the input file contains one integer  $h$  — the height of the skyscraper ( $1 \leq h \leq 10^{18}$ ).

The second line contains three integers  $a$ ,  $b$  and  $c$  — the parameters of the buttons ( $1 \leq a, b, c \leq 100\,000$ ).

### Output

Output one integer number — the number of floors that are reachable from the first floor.

### Example

<code>elevator.in</code>	<code>elevator.out</code>
15 4 7 9	9

## Problem F. Formula

Input file:            **formula.in**  
Output file:           **formula.out**  
Time limit:            2 seconds  
Memory limit:         64 megabytes

Nick is a mathematician and his speciality is Boolean logic, especially repetition-free functions. The Boolean function is repetition-free if it can be represented as a repetition-free formula. Formula is repetition-free if each variable occurs in the formula only once.

Let us fix the syntax of considered logical formulae:

- Variables — letters from ‘a’ to ‘k’;
- Parentheses — if  $E$  is a formula, then  $(E)$  is another;
- Negation —  $\neg E$  is a formula for any formula  $E$ ;
- Conjunction —  $E_1 \wedge E_2 \wedge \dots \wedge E_n$ .
- Disjunction —  $E_1 \vee E_2 \vee \dots \vee E_n$ .

The operations are listed from the highest priority to the lowest.

The problem is to represent given Boolean function by a repetition-free formula.

### Input

The only line of input contains the Boolean function represented as a string consisting of characters ‘a’..‘k’, ‘(’, ‘)’, ‘~’, ‘&’ and ‘|’. The last three tokens stand for  $\neg$ ,  $\wedge$  and  $\vee$  respectively. Tokens can be separated by an arbitrary number of spaces. The line contains 1 000 characters at most. The formula in the file is syntactically correct.

### Output

The first line of the output file must contain “Yes” if function is repetition-free and “No” otherwise.

In the former case the following line must contain the repetition-free formula for given Boolean function in the same format as in the input file. The line must contain no more than 1 000 characters.

### Example

formula.in	formula.out
(a   b) & (a   c)	Yes a   b & c
d&~d	No
d & ~d   ~((a ~b) & (a c))	Yes ~a&(b ~c)
a & b   ~ a & ~b	No

## Problem G. Given a string...

Input file:            **given.in**  
Output file:           **given.out**  
Time limit:            2 seconds  
Memory limit:         64 megabytes

Peter's Boss is now very upset. He said that Peter's vision of the orthogonal sum of two strings is not collinear to the general pary line of *RIGS*. At least, it is very bad that the orthogonal sum of two strings in Peter's vision can be different depending on a selected set of strings. But Boss decided to give Peter a last str... well, a chance.

Peter's colleague Andrew invented another definition of orthogonal sum of two strings of equal length  $n$ , which depends only on the alphabet. The basic alphabet to define this operation consists only of zeros and ones. The orthogonal sum of two strings  $a \oplus b$  is just a string  $c$  where  $c_i = a_i \oplus b_i$  ( $S_i$  denotes  $i$ -th character of string  $S$ ). Here  $\oplus$  stands for *exclusive OR* operation which returns 0 for equal characters and 1 otherwise.

Now Peter must study properties of *orthogonal closure* of a given string  $S$ . The orthogonal closure of  $S$  (denoted  $S^\oplus$ ) is a set of strings  $S_{(k)} \oplus S_{(l)}$  for any  $0 \leq k, l \leq n - 1$ , where  $n$  is the length of  $S$ , and  $S_{(k)}$  denotes an operation of *k-th circular shift* of  $S$  — moving  $k$  last characters from the end of the string  $S$  to its beginning. For example, the second circular shift of **abcde** is **deabc**.

Given a string  $T$ , Peter's task is to check whether it belongs to  $S^\oplus$ . Could you solve this task for him?

### Input

The first line of the input file contains a given string  $T$ . The second line contains  $S$ . Both strings are of equal length in range from 1 to 5 000 characters. All characters in these strings are zeros or ones.

### Output

If a given string belongs to  $S^\oplus$ , output "Yes". Otherwise output "No".

### Example

given.in	given.out
11111 10101	No
11110 10101	Yes

## Problem H. History of Football

Input file:            **history.in**  
Output file:           **history.out**  
Time limit:            2 seconds  
Memory limit:         64 megabytes

Henry is a historian. He specializes in the history of sports, especially football. Whenever he sees a table of a football tournament, he saves it into his database.

Recently he ran across a web-site with standings of a small tournament. Unfortunately for him, the results of the games were lost, and the only available information was the amount of points gained by each team.

Disappointed by that, he decides to have some mathematical fun and to calculate in how many different ways the games of the championship could have ended. He doesn't care about the scores of the games, he only cares about the winners.

In that tournament the following rules were applied:

- Each team plays against each other team exactly once.
- In case of a tie each team gains 1 point.
- In other case the winner gains 3 points and the loser gains 0 points.

For example, if Henry knows that each of 3 teams had got 3 points by the end of the tournament, the answer to his question is that there are two possible tournament tables:

Possible table number 1

Team	A	B	C	Points
A	-	3	0	3
B	0	-	3	3
C	3	0	-	3

Possible table number 2

Team	A	B	C	Points
A	-	0	3	3
B	3	-	0	3
C	0	3	-	3

Help Henry calculate the number of different possible tournament tables (without consideration of the scores of the games).

### Input

Input file contains integer  $n$ , the number of teams in the championship ( $2 \leq n \leq 8$ ). The following  $n$  lines contain one integer number each — points gained by the teams.

### Output

Output one integer number — the number of possible tournament tables with given total points. It is guaranteed that there is at least one such tournament table.

### Example

history.in	history.out
3	2
3	
3	
3	



## Problem I. iChess

Input file:            `ichess.in`  
Output file:          `ichess.out`  
Time limit:            2 seconds  
Memory limit:        64 megabytes

The Jury of *NEERC'07* quarterfinals is proud to present you a new game — chess patience. This patience is played not with cards, but with black and white square tiles. The goal of the game is to place these tiles on a flat surface so that they form a square colored in a chess-like pattern. The square should be totally filled and be of the maximal possible size. There may remain some spare tiles, if they do not fit into the resulting square.

To make this game more popular, a computer version of this patience named *iChess* was developed. The rules are the same with the exception that the player is given the number of tiles, not the actual tiles. Also, the result of the patience is not the actual layout, but the side length (measured in tiles) of the maximal square with the required layout.

Your task is to write a program which can play *iChess* patience.

### Input

The input file contains two integer numbers  $b$  and  $w$  — the number of black and white tiles respectively ( $0 \leq b, w \leq 10\,000$ ).

### Output

The first line of the input file must contain a single integer number  $s$  — the side length of the maximum possible square made of at most  $b$  black and  $w$  white tiles.

If no square can be formed with the given tiles, output a single word “Impossible”.

### Example

<code>ichess.in</code>	<code>ichess.out</code>
12 15	5
0 0	Impossible

## Problem J. Journey with Pigs

Input file:            journey.in  
Output file:           journey.out  
Time limit:            2 seconds  
Memory limit:         64 megabytes

Farmer John has a pig farm near town A. He wants to visit his friend living in town B. During this journey he will visit  $n$  small villages so he decided to earn some money. He took  $n$  pigs and plans to sell one pig in each village he visits.

Pork prices in villages are different, in the  $j$ -th village the people would buy a pork at  $p_j$  rubles per kilogram. The distance from town A to the  $j$ -th village along the road to town B is  $d_j$  kilometers.

Pigs have different weights. Transporting one kilogram of pork per one kilometer of the road needs  $t$  rubles for addition fuel.

Help John decide, which pig to sell in each town in order to earn as much money as possible.

### Input

The first line of the input file contains integer numbers  $n$  ( $1 \leq n \leq 1000$ ) and  $t$  ( $1 \leq t \leq 10^9$ ). The second line contains  $n$  integer numbers  $w_i$  ( $1 \leq w_i \leq 10^9$ ) — the weights of the pigs. The third line contains  $n$  integer numbers  $d_j$  ( $1 \leq d_j \leq 10^9$ ) — the distances to the villages from the town A. The fourth line contains  $n$  integer numbers  $p_j$  ( $1 \leq p_j \leq 10^9$ ) — the prices of pork in the villages.

### Output

Output  $n$  numbers, the  $j$ -th number is the number of pig to sell in the  $j$ -th village. The pigs are numbered from 1 in the order they are listed in the input file.

### Example

journey.in	journey.out
3 1	3 2 1
10 20 15	
10 20 30	
50 70 60	

## Problem K. K'ak'-u-pakal and Mayan Script

Input file: kak-u-pakal.in  
 Output file: kak-u-pakal.out  
 Time limit: 2 seconds  
 Memory limit: 64 megabytes

When scientists re-discovered ancient Mayan cities, they found many texts, written in unknown script. An example of the script is shown on the right, where the name of *K'ak'-u-pakal*, a military leader and priest in ancient Mayan city of *Chichén Itzá*, is written (see A. W. Voss, H. J. Kremer, *K'ak'-u-pakal, Hun-pik-tok' and the Kokom* for details). This hieroglyph can be found in many sites of the city.



Mayan hieroglyphs are not hieroglyphs in proper sense, but compositions of separate glyphs. All known glyphs (there is about one thousand of them) are indexed with numbers from 1 to 9999. A special language for encoding glyphs relative positions made it possible to write any hieroglyph in plain text. For example the above *K'ak'-u-pakal* hieroglyph is encoded as “((669:604).(586:(27:[(534.534)])))”.

Here is the formal grammar of the language (adapted for the contest):

$\langle \text{inscription} \rangle \rightarrow \langle \text{glyph id} \rangle | \langle ' \langle \text{block} \rangle ' \rangle | \langle ' \langle \text{block} \rangle : \langle \text{vertical group} \rangle ' \rangle$   
 $\langle \text{horizontal group} \rangle \rightarrow \langle \text{block} \rangle [ \langle ' \rangle \langle \text{horizontal group} \rangle ]$   
 $\langle \text{vertical group} \rangle \rightarrow \langle \text{block} \rangle [ \langle ' \rangle \langle \text{vertical group} \rangle ]$   
 $\langle \text{block} \rangle \rightarrow \langle \text{inscription} \rangle | \langle [ \langle \text{inscription} \rangle ] \rangle$

The hieroglyph encoding describes a process of the hieroglyph composition. Glyphs are combined horizontally or vertically (using ‘.’ or ‘:’) into blocks, which in turn are combined into larger and larger blocks, until the necessary configuration is achieved.

It took a hundred years to decipher Mayan hieroglyphs and convert them into plain text, but we hope that you can create a program for the backward conversion (text to hieroglyph layout) much quicker.

### Input

The first line of the input file contains a space-free text string (255 symbols at most), containing Mayan hieroglyph encoded in plain text form.

### Output

Output text, composed of characters ‘+’, ‘-’, ‘|’, ‘ ’ (ASCII codes 43, 45, 124, 32), ‘0’..‘9’ and line feeds. All blocks of a group should have exactly the same size, except the block with square braces around it (there will be one such block per group at most) which should be exactly two times wider (or higher if the group is vertical). The glyph id (with one leading and one trailing space) should be placed at the upper left corner of the block. The output should be as short as possible. It’s guaranteed that for each test there exists a proper layout, which has 100 000 bytes at most.

### Example

kak-u-pakal.in	kak-u-pakal.out
((669:604).(586:(27:[(534.534)])))	<pre> +-----+   669     586                       +-----+   604     27                +-----+           534    534                          +-----+                     </pre>