# Problem A. Cartesian Tree (Treap)

Input file: system input
Output file: system output
Time limit: 1 seconds
Memory limit: 256 megabytes

Given pairs of integers  $(a_i, b_i)$  your task is to build a treap such that *i*-th node has keys  $(a_i, b_i)$ . Nodes with keys  $a_i$  must satisfy binary search tree constraints and nodes with keys  $b_i$  must satisfy heap constraints.

#### Input

The first line contains single integer N ( $1 \le N \le 50\,000$ ) — the number of pairs. The following N lines contain pairs  $(a_i, b_i)$ . For all pairs  $|a_i|, |b_i| \le 30\,000$  and  $a_i \ne a_j$  for all  $i \ne j$ .

## Output

If the treap with this set of keys does not exist, output NO in the first line. Otherwise, the first line must contain word YES and the following N lines must describe nodes of the treap. A node is described with three integers: number of the ancestor, number of the left child and number of the right child. If node does not have ancestor or some of child, output zero instead missing node.

# Example

system input	system output
7	YES
5 4	2 3 6
2 2	0 5 1
3 9	1 0 7
0 5	5 0 0
1 3	2 4 0
6 6	1 0 0
4 11	3 0 0

# **Problem B. Binary Search Tree**

Input file: system input
Output file: system output
Time limit: 2 seconds
Memory limit: 256 megabytes

Your task is to implement a binary search tree.

#### Input

The input file contains descriptions of queries performed on the tree. Number of queries does not exceed 100 000. Each line of the input file contains one of the following query:

- insert x insert a key x into the tree.
- $delete \ x$   $delete \ a \ key \ x$  from the tree.
- exists x if there is key x in the tree, output "true", otherwise, output "false".
- $next\ x$  output minimal element in the tree that strictly greater than x. If there is no such element, output "none".
- $prev\ x$  output maximal element in the tree that strictly less than x. If there is no such element, output "none".

The integers in the all queries do not exceed  $10^9$  by the absolute value.

#### Output

Output the results of the execution of all queries *exists*, *next* and *prev* from the input file. Follow the format of the output file in the example.

## Example

system input	system output
insert 2	true
insert 5	false
insert 3	5
exists 2	3
exists 4	none
next 4	3
prev 4	
delete 5	
next 4	
prev 4	

## Problem C. K-th Maximum

Input file: system input
Output file: system output
Time limit: 2 seconds
Memory limit: 64 megabytes

Your task is to implement the data structure that allows to add and remove elements and also to find the k-th maximum.

#### Input

The first line contains an integer n ( $1 \le n \le 100\,000$ ) — the number of queries. Each of the following n line contains a description of the query. Every query is described by two integers  $c_i$  and  $k_i$  — the type and argument of query, respectively ( $|k_i| \le 10^9$ ). The allowing commands are:

- +1 (or simply 1): add an element with the key  $k_i$ ;
- 0: output the k-th maximum;
- -1: remove the element with the key  $k_i$ .

It is guaranteed that it does not need to keep elements with equal keys and remove nonexistent element. Also, it is guaranteed that the  $k_i$ -th maximum exists, when it is requested.

## Output

For every command of type 0 output a single integer — the result of the query.

## **Example**

system input	system output
11	7
+1 5	5
+1 3	3
+1 7	10
0 1	7
0 2	3
0 3	
-1 5	
+1 10	
0 1	
0 2	
0 3	

#### Problem D. Sum

Input file: system input
Output file: system output
Time limit: 3 seconds
Memory limit: 256 megabytes

Consider a set S of integers. Your task is to implement the data structure that allows the following queries:

• add(i) — add value i at the set S (if i is already in S, nothing happens);

• sum(l,r) — output sum of all elements x from S satisfying the inequalities  $l \le x \le r$ .

#### Input

Initially the set S is empty. The first line contains an integer n  $(1 \le n \le 300\,000)$  — the number of queries. Each of the following n lines contains a description of the commands. Every line is either "+ i" or "? l r". The line "? l r" issues the query sum(l,r). If the line "+ i" is either at the beginning of the input file or after another line starting with "+", this line issues query add(i). Otherwise, if this line follows the line starting with "?" and the result of the previous query was y, it issues query add(i).

Arguments of every query belong to the interval from 0 to  $10^9$ .

#### Output

For every line starting with "?" output a single number — the result of the corresponding query.

#### Example

system input	system output
6	3
+ 1	7
+ 3	
+ 3	
? 2 4	
+ 1	
? 2 4	

# Problem E. Implicit Key

Input file: system input
Output file: system output
Time limit: 1 seconds
Memory limit: 256 megabytes

Your task is to implement the data structure that allows to perform the following queries on the array:

- add i x add the element x after the i-th element of the array  $(0 \le i \le len)$ ;
- del i remove the *i*-th element of the array.

#### Input

The first line contains two integers n and m  $(1 \le n, m \le 10^5)$  — the length of the initial array and the number of queries. The second line contains n integers — the elements of the initial

array. All elements belong to the interval from 0 to  $10^9 - 1$ . The following m lines contain **Example** description of the queries as described above. It is guaranteed that all queries are correct. That means, for example, that i-th element exists, when it is requested to be removed.

#### Output

Output the final state of the array. The first line must contain the single integer — length of the array. The second line must contain the elements of the array separated by space.

#### Example

system input	system output
3 4	3
1 2 3	9 2 8
del 3	
add 0 9	
add 3 8	
del 2	

# Problem F. Range Minimum Query

Input file: system input Output file: system output Time limit: 2 seconds Memory limit: 256 megabytes

The Giggle company opens new office in France and you are invited for an interview. Your task is to implement the data structure that allows to perform two queries on the array:

- ?ix return the minimum element in the range from i to i:
- +ix insert an element x after the i-th element of the array. If i=0 then element is inserted at the beginning of the array.

Initially vhe array is empty.

# Input

The first line contains single integer n ( $1 \le n \le 200000$ ) — the number of the queries.

The following n lines contain the description of the queries as described above. It is guaranteed that all queries are correct. All values of the elements in the array do not exceed 109 by the absolute value.

# Output

For every query of the first kind output its result on the separate line.

system input	system output
8	4
+ 0 5	3
+ 1 3	1
+ 1 4	
? 1 2	
+ 0 2	
? 2 4	
+ 4 1	
? 3 5	

# Problem G. Swapper

Input file: system input Output file: system output Time limit: 2 seconds Memory limit: 256 megabytes

Before returning to the headquarters Aahz and Skeeve had to fill declaration in local customs. The result was a quite enormous sequence of numbers. It takes a lot of time to process this sequence.

- Swapper is bad, customs official said knowledgeably.
- What is swapper? curious Skeeve asked.

Ashz explained that swapper is data structure allowed the following queries

- in the range from x to y with even length (y-x+1) is divisile by 2) swap elements x with x + 1, x + 2 with x + 3 and so on;
- calculate the sum in the arbitrary range.

Calculation can take a long time, so Myth corporation asks you to solve problem with swapper. Your task is to simulate queries effectively.

# Input

The input file contains one or several tests. The first line of every test contains two integers nand m ( $1 \le n, m \le 100000$ ) — the length of sequence and the number of queries. The second line of test contains n integers — the sequence. Every element of this sequence does not exceed 10<sup>6</sup> by the absolute value.

Each of the following m lines contains a description of a query. A query of both kinds is defined with three integers: 1  $x_i$   $y_i$  for a query of the first kind, and 2  $a_i$   $b_i$  for a query of the second kind. Sum over all n and m in the input file does not exceed 200 000. The input file ends with the string of two zeros. It is guaranteed  $x_i < y_i$  and  $a_i < b_i$ .

#### Output

For every test output responses to queries of the second type as shown in the example. The responses for different tests must be separated with empty line.

# Example

system input	system output
5 5	Swapper 1:
1 2 3 4 5	10
1 2 5	9
2 2 4	2
1 1 4	
2 1 3	
2 4 4	
0 0	

## Problem H. Move To Front!

Input file: system input
Output file: system output
Time limit: 6 seconds
Memory limit: 256 megabytes

Corporal Ducar enjoys to give commands to his troops. His favorite command is "Move to front!". Corporal aligns his soldiers in a row and gives some commands. Each of them is formulated as "Soldiers from l to r, move to front!". Before Ducar gave the first command, the soldiers had been numbered from 1 to n, from left to right. When soldiers hear a command "Soldiers from l to r, move to front!", soldiers with numbers from l to r move to the beginning of the row in the same order in which they are.

For example, if at some moment in time the soldiers stand in an order 1, 3, 6, 2, 5, 4, then after the command "Soldiers from 2 to 3, move to front!" the new order is 3, 6, 1, 2, 5, 4. If soldiers from 3 to 4 are moved to front by next command of corporal, than new order is already so 1, 2, 3, 6, 5, 4.

Given the sequence of the commands of the corporal, your task is to find the order of soldiers after all commands.

## Input

The first line contains two integers n and m ( $1 \le n \le 100\,000$ ,  $1 \le m \le 100\,000$ ) — the number of the soldiers and the number of commands, respectively. Each of the following m line contains description of the commands: two integers  $l_i$  and  $r_i$  ( $1 \le l_i \le r_i \le n$ ).

#### Output

The single line must contain n integers — the order of the soldiers after the execution of all commands.

## Example

system input	system output
6 3	1 4 5 2 3 6
2 4	
3 5	
2 2	

#### Problem I. Reverse

Input file: system input
Output file: system output
Time limit: 5 seconds
Memory limit: 256 megabytes

Physical education teacher has learned to count the total height of all students staying in a row on the positions from l to r a long time ago. But children play a trick on him. At some moments the children in positions from l to r are swapped. The teacher noticed that they always "reverse" the segment. That means l-th student swaps with r-th student, (l+1)-th student swaps with (r-1)-th student and so on. He decided not to scold them, but to count the total height on all scheduled intervals.

## Input

The first line contains two integers n and m ( $1 \le n, m \le 200\,000$ ) — the number of children and the number of events. The second line contains n natural numbers — the heights of children in the order in the row. The height of every child does not exceed  $2 \cdot 10^5$ . Each of the following m lines contains a description of an event: three numbers q, l, r ( $0 \le q \le 1$ ,  $1 \le l \le r \le n$ ). The number q represents a type of the event: 0 corresponds to a query to calculate the total height of children with numbers from l to r, 1 shows that children with numbers from l to r "reverse" their interval. All numbers in the input file are integers.

## Output

For every event of kind 0 output a single number on the separate line — an answer for this query.

## **Example**

system input	system output
5 6	15
1 2 3 4 5	9
0 1 5	8
0 2 4	7
1 2 4	10
0 1 3	
0 4 5	
0 3 5	

# Problem J. Key Values

Input file: system input
Output file: system output
Time limit: 2 seconds
Memory limit: 64 megabytes

You are employed by MacroHard company and as the first task they asked to implement new data structure. It should allow to keep integer key values.

This structure represents an array A of infinity length. Cells of this array are numbered starting from one. Initially, all cells are empty. The only query that data stucture allows is Insert(L, K) where L is the position in the array and K is some positive integer key value. The query is performed in the following way:

- if cell A[i] is empty, assign A[L] := K;
- otherwise, if cell A[i] is not empty, execute Insert(L+1, A[L]) and after execution assign A[L] := K.

Given the sequence of n integers  $L_1, L_2, \ldots, L_n$  your task is to output the content of this array after execution the following queries:

 $Insert(L_1, 1)$ 

 $Insert(L_2, 2)$ 

. . .

 $Insert(L_N, N)$ 

## Input

The first line contains two integers N and M ( $1 \le N \le 131\,072$ ,  $1 \le M \le 131\,072$ ) — the number of queries and the maximal index that is allowed to use in *Insert* query. The following line contains n integers  $L_i$  — the description of *Insert* queries ( $1 \le L_i \le M$ ).

#### Output

Output the content of the array after the execution of the given sequence of queries. The first line must contain integer W — index of the last non-empty cell. The second line must contain W integers —  $A[1], A[2], \ldots, A[W]$ . Output zero if cell is empty.

#### Example

system input	system output
5 4	6
3 3 4 1 3	4 0 5 2 3 1

## **Problem K. Log Analysis**

Input file: system input
Output file: system output
Time limit: 2 seconds
Memory limit: 256 megabytes

Lisa writes a log analysis application for a distributed computer system. Unlike single-node logs, that are append-only the distributed log is highly volatile. When a node becomes online, it may push a batch of events in the past of the log. Conversely, when it goes offline some log entries may disappear.

To ensure the stability and availability of the application Lisa needs to monitor the number of distinct events in the log segments. She is going to handle distributed part, while you have to implement a local one.

Your program is started from the empty log and must support the following operations:

- insert  $\langle index \rangle \langle number \rangle \langle type \rangle$  inserts  $\langle number \rangle$  of events of type  $\langle type \rangle$  before event with index  $\langle index \rangle$ . Events with indices larger or equal to  $\langle index \rangle$  are renumbered.
- remove  $\langle index \rangle \langle number \rangle$  removes  $\langle number \rangle$  of events starting from event with index  $\langle index \rangle$ .
- query  $\langle index_1 \rangle$   $\langle index_2 \rangle$  counts the number of distinct event types for events with indices from  $\langle index_1 \rangle$  to  $\langle index_2 \rangle$  inclusive.

The events are indexed starting from 1. The event types are represented by single-letter codes.

# Input

The first line of the input file contains single integer number n — the number of operations (1 < n < 30 000). The following n lines contain one operation description each.

Operation description starts with operation type: '+' for insert, '-' for remove and '?' for query. Operation type is followed by operation arguments.

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All indices are valid, i. e. events with specified indices exist, and you never have to remove events past the end of the log.

The  $\langle number \rangle$  for the insert and remove operations does not exceed 10 000.

Event types are represented by lowercase Latin letter.

#### Output

For each query operation output a single number — the number of distinct event types between  $\langle index_1 \rangle$  and  $\langle index_2 \rangle$  inclusive.

## **Examples**

system input	system output
8	2
+ 1 4 w	1
+ 3 3 0	3
? 2 3	
- 2 2	
? 2 3	
+ 2 2 t	
? 1 6	
- 1 6	

#### Problem L. Cartesian Trees

Input file: system input
Output file: system output
Time limit: 3 seconds
Memory limit: 256 megabytes

Recently, on a lecture Vasya learn about Cartesian trees. Cartesian tree is a binary tree, in which each node contains two integers: key and priority. The tree is a search tree by the set of keys and is a heap by the priories, i.e.:

- the key of each node in the left subtree of node v is less than the key in v:
- the key of each node in the right subtree of node v is bigger than the key in v;
- priorities of the chidren of node v are not bigger than priority of v.

On the exam he received the following problem: you are given n pairs (key, priority), i-th of them looks like  $(i, y_i)$ , and you has to calculate the number of ways to build a Carteian tree, using as key of vertex i the number i, and  $y_i$  as priority. Because this number could be big enough, find the result modulo  $10^9 + 7$ .

Two Cartesian trees are different, if they have different roots, or there exists a vertex that has different parents in both trees.

#### Input

The first line of the input contains one integer t — the number of tests in the input. Then the description of each test follows.

Each description consists of two lines. The first line contains one integer n  $(1 \le n \le 10^5)$  — the number of nodes in the tree. The second line contains n integers  $y_i$   $(1 \le y_i \le 10^9)$  — the priority of the i-th node.

The sum of n does not exceed  $2 \cdot 10^5$ .

#### Output

For each test output the number of different Cartesian trees, that could be built on the given priorities, modulo  $10^9 + 7$ , on a separate line.

#### **Examples**

system input	system output
2	1
4	10
2 4 1 3	
6	
7 3 3 1 1 3	