

# ACM ICPC SOUTH PACIFIC REGIONALS

NOVEMBER 26, 2016

## **Contest Problems**

- A: Anticlockwise Motion
- B: Balloon Warehouse
- C: Crazy Rotations
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- E: Election Frenzy
- F: False Intelligence
- G: Graphics Design
- H: Hilbert's Hash Browns
- I: Intuidiff II
- J : Just Terraffic!
- K: Kiwis vs Kangaroos



This contest contains eleven problems. The top teams will advance to the ACM-ICPC World Finals 2017.

Judging team:

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## Problem A Anticlockwise Motion Time limit: 1 second

You have come up with an idea for a board game. The game is played on a board that is made up of  $32\,001 \times 32\,001$  numbered squares. The centre square contains the number 1 and the other numbers are arranged in an anticlockwise spiral outwards (first moving downwards, then to the right, then upwards, then to the left, then downwards again, and so on). Figure A.1 displays the  $5 \times 5$  squares in the middle of the board and Figure A.2 displays the  $21 \times 21$  squares in the middle of the board for further clarification. When playing the game, players will only be able to move up, left, down and right. To help work out the rules for the game, you would like to know the shortest distance between two squares on the board using only these moves.

#### $\mathbf{21}$ $\mathbf{20}$ 1918 17227 6 $\mathbf{5}$ 1623 8 151 4 $\mathbf{2}$ $\mathbf{24}$ 9 3 14 25 10 11 1213

### Input

The input consists of a single line containing two integers a  $(1 \le a \le 10^9)$ , which is the starting square, and b  $(1 \le b \le 10^9)$ , which is the ending square.

## Output

Display the shortest distance between a and b.

| Sample Input 1 | Sample Output 1 |
|----------------|-----------------|
| 12 2           | 2               |
|                |                 |
| Sample Input 2 | Sample Output 2 |

Figure A.1: The middle 25 squares.



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| 421 | 420 | 419 | 418 | 417 | 416 | 415 | 414 | 413 | 412 | 411 | 410 | 409 | 408 | 407 | 406 | 405 | 404 | 403 | 402 | 401 |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 422 | 343 | 342 | 341 | 340 | 339 | 338 | 337 | 336 | 335 | 334 | 333 | 332 | 331 | 330 | 329 | 328 | 327 | 326 | 325 | 400 |
| 423 | 344 | 273 | 272 | 271 | 270 | 269 | 268 | 267 | 266 | 265 | 264 | 263 | 262 | 261 | 260 | 259 | 258 | 257 | 324 | 399 |
| 424 | 345 | 274 | 211 | 210 | 209 | 208 | 207 | 206 | 205 | 204 | 203 | 202 | 201 | 200 | 199 | 198 | 197 | 256 | 323 | 398 |
| 425 | 346 | 275 | 212 | 157 | 156 | 155 | 154 | 153 | 152 | 151 | 150 | 149 | 148 | 147 | 146 | 145 | 196 | 255 | 322 | 397 |
| 426 | 347 | 276 | 213 | 158 | 111 | 110 | 109 | 108 | 107 | 106 | 105 | 104 | 103 | 102 | 101 | 144 | 195 | 254 | 321 | 396 |
| 427 | 348 | 277 | 214 | 159 | 112 | 73  | 72  | 71  | 70  | 69  | 68  | 67  | 66  | 65  | 100 | 143 | 194 | 253 | 320 | 395 |
| 428 | 349 | 278 | 215 | 160 | 113 | 74  | 43  | 42  | 41  | 40  | 39  | 38  | 37  | 64  | 99  | 142 | 193 | 252 | 319 | 394 |
| 429 | 350 | 279 | 216 | 161 | 114 | 75  | 44  | 21  | 20  | 19  | 18  | 17  | 36  | 63  | 98  | 141 | 192 | 251 | 318 | 393 |
| 430 | 351 | 280 | 217 | 162 | 115 | 76  | 45  | 22  | 7   | 6   | 5   | 16  | 35  | 62  | 97  | 140 | 191 | 250 | 317 | 392 |
| 431 | 352 | 281 | 218 | 163 | 116 | 77  | 46  | 23  | 8   | 1   | 4   | 15  | 34  | 61  | 96  | 139 | 190 | 249 | 316 | 391 |
| 432 | 353 | 282 | 219 | 164 | 117 | 78  | 47  | 24  | 9   | 2   | 3   | 14  | 33  | 60  | 95  | 138 | 189 | 248 | 315 | 390 |
| 433 | 354 | 283 | 220 | 165 | 118 | 79  | 48  | 25  | 10  | 11  | 12  | 13  | 32  | 59  | 94  | 137 | 188 | 247 | 314 | 389 |
| 434 | 355 | 284 | 221 | 166 | 119 | 80  | 49  | 26  | 27  | 28  | 29  | 30  | 31  | 58  | 93  | 136 | 187 | 246 | 313 | 388 |
| 435 | 356 | 285 | 222 | 167 | 120 | 81  | 50  | 51  | 52  | 53  | 54  | 55  | 56  | 57  | 92  | 135 | 186 | 245 | 312 | 387 |
| 436 | 357 | 286 | 223 | 168 | 121 | 82  | 83  | 84  | 85  | 86  | 87  | 88  | 89  | 90  | 91  | 134 | 185 | 244 | 311 | 386 |
| 437 | 358 | 287 | 224 | 169 | 122 | 123 | 124 | 125 | 126 | 127 | 128 | 129 | 130 | 131 | 132 | 133 | 184 | 243 | 310 | 385 |
| 438 | 359 | 288 | 225 | 170 | 171 | 172 | 173 | 174 | 175 | 176 | 177 | 178 | 179 | 180 | 181 | 182 | 183 | 242 | 309 | 384 |
| 439 | 360 | 289 | 226 | 227 | 228 | 229 | 230 | 231 | 232 | 233 | 234 | 235 | 236 | 237 | 238 | 239 | 240 | 241 | 308 | 383 |
| 440 | 361 | 290 | 291 | 292 | 293 | 294 | 295 | 296 | 297 | 298 | 299 | 300 | 301 | 302 | 303 | 304 | 305 | 306 | 307 | 382 |
| 441 | 362 | 363 | 364 | 365 | 366 | 367 | 368 | 369 | 370 | 371 | 372 | 373 | 374 | 375 | 376 | 377 | 378 | 379 | 380 | 381 |

Figure A.2: The middle 441 squares.



Figure B.1: An infinitely long line of balloons

Darcy has taken over management of a balloon warehouse. Unfortunately, it stocks an infinite supply of balloons, so he has requested your help! At the start of today, the warehouse consists of an infinitely long line of white balloons. In this problem, we describe a coloured balloon by an integer whose value uniquely represents a particular colour, so initially (taking 0 to mean a white balloon) the contents of the line is given by

0 0 0 ...

Specific balloons are identified by their 0-indexed position in the line starting from the front of the line (0, 1, 2, ...).

Throughout the day, Darcy receives n deliveries of balloons from his supplier. The *i*th delivery consists of an infinite number of balloons of colour y and comes with the instruction (x, y). If there are any balloons of colour x in the line, then he should insert exactly one balloon of colour y into his infinitely long line immediately after each balloon of colour x already present in the line. Otherwise, he will send the balloons of colour y back.

After all the deliveries of the day are completed, Darcy receives one final instruction from his supplier to check if he has properly followed the instructions he was given: what colour are all the balloons in the positions between l (inclusive) and r (exclusive) in the line? You should help Darcy answer this question.

Consider an example day with four deliveries (0, 1), (1, 3), (0, 1), (1, 2) (for example, it may be that 1 means a blue balloon, 2 means a red balloon and 3 means a green balloon; 0 is white as above). At the end of the day, Darcy's line resembles the line of balloons in Figure B.1; we describe it by

 $0 \ 1 \ 2 \ 1 \ 2 \ 3 \ 0 \ 1 \ \dots$ 

If he is asked for  $\ell = 1$  and r = 6, he should report the numbers 1 2 1 2 3 corresponding to blue, red, blue, red and green balloons in those positions in order.

### Input

The first line of the input contains three integers  $n \ (1 \le n \le 200\ 000)$ , which is the number of deliveries,  $\ell$  and  $r \ (0 \le \ell < r \le 10^6 \text{ and } r - \ell \le 100\ 000)$ , which are the positions between which to report the balloons' colours at the end of the day.

The next n lines describe the deliveries. Each of these lines contain two distinct integers x ( $0 \le x < 200\,000$ ) and y ( $0 \le y < 200\,000$ ), which is the instruction for this delivery.

### Output

Display the colours of the balloons between positions  $\ell$  (inclusive) and r (exclusive).



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| Sample Input 1 | Sample Output 1 |
|----------------|-----------------|
| 4 1 6          | 1 2 1 2 3       |
| 0 1            |                 |
| 1 3            |                 |
| 0 1            |                 |
| 1 2            |                 |

| Sample Input 2  | Sample Output 2 |  |  |  |
|-----------------|-----------------|--|--|--|
| 1 101000 101008 | 0 1 0 1 0 1 0 1 |  |  |  |
| 0 1             |                 |  |  |  |



## Problem C Crazy Rotations Time limit: 1 second

Cynthia has a long line of n coloured lights. These lights will be animated by rotating the colours of the lights. To rotate the colours by k spots, the colour of light i at time t is the same as the colour of light  $(i - k) \mod n$  at time t - 1. When Cynthia does this, there may be several lights that change colour. The *craziness* of a rotation by k spots is the number of lights that change colour. For example, in Figure C.1, rotating the colours by one spot changes the colour of six lights, so the craziness of this rotation is 6.

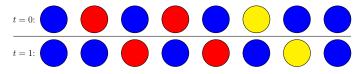


Figure C.1: Rotation by one spot.

Cynthia wishes to create an *insane sequence*, which is a sequence of n-1 different rotations so that the craziness never decreases. To be specific, an insane sequence is a permutation  $(p_1, p_2, \ldots, p_{n-1})$  of the first n-1 positive integers such that the craziness of a rotation by  $p_{i-1}$  spots is not more than the craziness of a rotation by  $p_i$  spots for all  $i (2 \le i < n)$ . Figure C.2 is an example of an insane sequence.

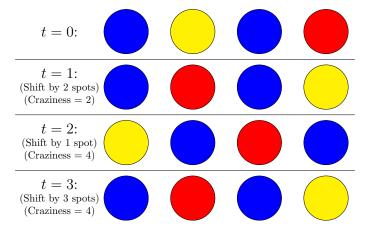


Figure C.2: An insane sequence of rotations (with the permutation 2, 1, 3).

In Figure C.2, a shift of 1 is in the second location (t = 2) of the insane sequence. Given the initial colours of the lights and an integer p, what is the smallest positive integer that can be in the pth location (t = p) of an insane sequence?

### Input

The first line of input contains two integers  $n \ (2 \le n \le 500\ 000)$ , which is the number of lights, and  $p \ (1 \le p < n)$ , which is the location in the sequence that we are interested in.

The second line contains a string of length n, which is the initial configuration of the lights. Each light's colour is identified by a single character ( $\mathbb{R}$  for red,  $\mathbb{B}$  for blue or  $\mathbb{Y}$  for yellow).





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## Output

Display the smallest number that could be in the *p*th location of an insane sequence.

| Sample Input 1 | Sample Output 1 |  |
|----------------|-----------------|--|
| 4 2            | 1               |  |
| BYBR           |                 |  |
|                |                 |  |
| <u></u>        |                 |  |
| Sample Input 2 | Sample Output 2 |  |
| Sample Input 2 | Sample Output 2 |  |



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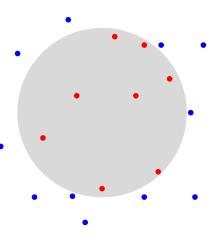
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## Problem D Dendroctonus Time limit: 1 second

Mountain pine beetles (Dendroctonus ponderosae) are small pests that bore into trees and cause a huge amount of damage. Recently, a large increase in their population has occurred and scientists would like some more information about the origin of the outbreak(s). In particular, they want to know if there was a single outbreak or multiple outbreaks. If there is more than one outbreak, then they must raise the alert level.

For each outbreak, the beetles start at a single location (known as the initial infection point) and slowly work their way outwards. If a tree is inside the infection area, then it is infected. If a tree is outside of the infection area, then it is not infected. If a tree is on the boundary of the infection area, then it may or may not be infected. The infection area is always a circle centred at the initial infection point.

Given the locations of the infected and non-infected trees, the scientists need you to determine if there is enough evidence to raise the alert level.



### Input

The first line of the input contains a single integer n ( $1 \le n \le 100$ ), which is the number of trees.

The next n lines describe the trees. Each of these lines contains two integers x (-250  $\leq x \leq$  250) and y (-250  $\leq y \leq$  250), which is the location of the tree, as well as a single character p (I or N), denoting if the tree is infected or not. If p is I, then the tree is infected. If p is N, then the tree is not infected. Trees are single points on the plane. Note that the initial infection point for an outbreak does not need to be a tree and does not have to be at an integer location. The n trees are at distinct locations.

## Output

If it is guaranteed that there is more than one outbreak, display Yes. Otherwise, display No.

| Sample Input 1 | Sample Output 1 |  |
|----------------|-----------------|--|
| 7              | No              |  |
| 0 0 I          |                 |  |
| 1 0 I          |                 |  |
| 0 1 I          |                 |  |
| 4 4 N          |                 |  |
| 4 -4 N         |                 |  |
| -4 4 N         |                 |  |
| -4 -4 N        |                 |  |







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| Sample Input 2 | Sample Output 2 |  |
|----------------|-----------------|--|
| 10             | Yes             |  |
| 5 1 I          |                 |  |
| 5 -1 I         |                 |  |
| 6 4 N          |                 |  |
| 6 -4 N         |                 |  |
| 0 2 N          |                 |  |
| 0 -2 N         |                 |  |
| -5 1 I         |                 |  |
| -5 -1 I        |                 |  |
| -6 4 N         |                 |  |
| -6 -4 N        |                 |  |



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## Problem E Election Frenzy Time limit: 1 second

Checks and balances are some of the most important parts of any democratic government system. After a long campaign, the election between Phong, from the Sprites Party, and Megabyte, from the Viruses Party, has just finished. The only thing left to do is count the votes and declare a winner.

The votes are counted in a room with t tables. At each table, there is a person counting votes. These people are called *counters*. Members from the two political parties are allowed to be in the room to ensure that the counting is done fairly. These people are called *scrutineers*. In a perfect system, one scrutineer from each political party would be present at each table. Unfortunately, this is not possible since there is only enough room for one scrutineer per table.



Source: Reboot Wil

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We need your help in deciding how to assign the scrutineers to the tables. Each table must have exactly one scrutineer: from either the Sprites or the Viruses. Some of the tables are close to one another. This means that a scrutineer will be able to monitor the counting at their table and all surrounding tables. An assignment of scrutineers is considered fair if every table is monitored by at least one Sprite and at least one Virus.

The counter at each table was asked to submit a list of all tables that can be seen from their table. For some reason, some of the counters submitted a list of the tables that *can* be seen from their table and some of the counters submitted a list of tables that *cannot* be seen from their table.

Given this information, find a fair assignments of scrutineers.

#### Input

The first line of input contains a single integer t ( $1 \le t \le 200\,000$ ), which is the number of tables.

The next t lines describe the lists that the counters submitted for each table. Each of these lines starts with a letter p (either C or N), which is the type of the list, and an integer k ( $0 \le k \le t - 1$ ), which is the length of the list. This is followed by k distinct integers  $a_1, \ldots, a_k$  ( $1 \le a_i \le n$ ), which are the items on the list. If p = C, then each table  $a_i$  can be monitored by the scrutineer at this table and all other tables cannot be monitored. If p = N, then each table  $a_i$  cannot be monitored by the scrutineer at this table and all other tables can be monitored. The list does not contain its own table number since the scrutineer can always monitor the table they are sitting at.

The first table in the input is table 1, the second table is table 2, and so on. It is guaranteed that if table x can monitor table y, then table y can monitor table x. The total length of all lists is at most 500 000.

### Output

Display any fair assignment of scrutineers. The assignment should be described as a string of length t containing only the letters S, for a Sprite scrutineer, and V, for a Virus scrutineer. The first letter of the string is the scrutineer for table 1, the second letter is the scrutineer for table 2, and so on. If there are multiple solutions, display any of them. If there is no such assignment, display Impossible instead.



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| Sample Input 1 | Sample Output 1 |
|----------------|-----------------|
| 5              | SSVVV           |
| C 3 3 4 5      |                 |
| C 3 3 4 5      |                 |
| C 2 1 2        |                 |
| C 2 1 2        |                 |
| C 2 1 2        |                 |
| ·              | '               |

| Sample Input 2 | Sample Output 2 |
|----------------|-----------------|
| 4              | SSVV            |
| C 2 2 4        |                 |
| N 1 4          |                 |
| N 2 1 4        |                 |
| C 1 1          |                 |
|                |                 |

| Sample Input 3 | Sample Output 3 |
|----------------|-----------------|
| 1              | Impossible      |
| N 0            |                 |



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## Problem F False Intelligence Time limit: 1 second

Artificial Intelligence is taking over the world, or at least planning to do so soon. Machines will become so clever they can win all games, answer all your questions and make all decisions for you. Because this sounds quite scary, it has been proposed to give the machines a bit of human touch. This feature will make them pretend to not always know the answer to a question, but to express uncertainty from time to time.

Of course, secretly, the machines will still follow precise rules – those of three-valued logic invented by Jan Łukasiewicz. It adds to the two values F (false) and T (true) of Boolean logic a third value U (uncertain) and extends the logic operators as shown in the first three of the following tables:



Source: Hiroaki Maeda, Flickr CC BY-ND 2.0

| ∧ F U T                       | V FUT                         | $\rightarrow$ F U T           | _ ≡   F U T                   |
|-------------------------------|-------------------------------|-------------------------------|-------------------------------|
| F F F F<br>U F U U<br>T F U T | F F U T<br>U U U T<br>T T T T | F T T T<br>U U T T<br>T F U T | F T F F<br>U F T F<br>T F F T |
| AND                           | OR                            | IMPLIES                       | EQUALS                        |

For example,  $F \lor T = T$  as in Boolean logic,  $T \land U = U$  and  $F \rightarrow U = T$ . Some functions cannot be expressed using the three operators AND, OR and IMPLIES. For example,  $f(x, y) = x \rightarrow x$  is the constant T function, but there is no expression q(x, y) in terms of x, y, AND, OR and IMPLIES which is constant F.

Let us add the operator EQUALS shown in the right-most of the above tables. It captures equality of its two arguments by returning T if they are the same and F otherwise. Your task is to determine whether a given function g(x, y) can be expressed in terms of x, y, AND, OR, IMPLIES and EQUALS. This is important so the machines know their own limits.

### Input

The first line of the input contains an integer n ( $1 \le n \le 20000$ ), which is the number of functions you have to consider. This is followed by n function descriptions.

Each function description consists of four lines. The first of these lines is empty. The remaining three lines describe a function g as a table of its values g(x, y). The table has three rows and three columns, corresponding to the values F, U, T of x and y, respectively. Its layout is like that of the tables shown above.

## Output

For each function description in the same order as in the input, display one line containing either definable or undefinable. Display definable if the given function g(x, y) can be expressed in terms of x, y, AND, OR, IMPLIES and EQUALS. Display undefinable if g(x, y) cannot be expressed this way.







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| Sample Input 1 | Sample Output 1 |
|----------------|-----------------|
| 3              | definable       |
|                | definable       |
| FFF            | undefinable     |
| FUU            |                 |
| FUT            |                 |
|                |                 |
| ТТТ            |                 |
| UUT            |                 |
| FUT            |                 |
|                |                 |
| ТТТ            |                 |
| 000            |                 |
| FFF            |                 |



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## Problem G Graphics Design Time limit: 1 second

You are in a graphics design course. You and the rest of your class need to finish your final projects. The instructor has several items (cameras, camcorders and super computers) that the students will use to finish their projects. Each project consists of several subprojects that must be completed in order. These subprojects may or may not be different for each student. Each subproject may need a camera, a camcorder and/or a super computer (8 possibilities). The instructor has given each subproject a number, its priority.

A subproject is eligible to be started if all items that are needed for that subproject are available and the student has fully completed all of their sub-



projects before this one. Out of all eligible subprojects, the one with the highest priority will be started first. This student will borrow the items needed to complete the subproject and then return them after the subproject is finished.

If, after a subproject has started and the items have been borrowed, there still remain eligible subprojects, the eligible subproject with the highest priority is started. This means that it is possible that several subprojects are started at the same time (see Sample Input 1). It is also possible that several students are waiting for an item to be returned, and so there are no eligible subprojects at a specific moment in time (see Sample Input 2). Note that the order of each student's subprojects is fixed. That is, they must complete their first subproject first, then their second subproject, and so on, even if the priorities of their subprojects are not in decreasing order (see Sample Input 3).

If a student starts a subproject at time x and it takes t time units to complete, then the subproject is considered finished at time x + t and the student must return the borrowed items. This means that the items borrowed for that subproject are available to be borrowed again at time x + t and that the student is able to start their next subproject at time x + t (subject to availability of the items and the subproject's priority, as specified above). Each camera, camcorder and super computer can only be used by one student at a time. Students must do the subprojects in order, even if they have the items needed for a later subproject but not the current one.

For each student, you are to compute the time that they finish their last subproject.

#### Input

The first line of input contains a single integer n  $(1 \le n \le 1000)$ , which is the number of students in the class. The second line contains 3 integers a  $(1 \le a \le 1000)$ , which is the number of cameras available, b  $(1 \le b \le 1000)$ , which is the number of cameras available, b  $(1 \le b \le 1000)$ , which is the number of super computers available. The third line contains n integers  $d_1, \ldots, d_n$   $(1 \le d_i \le 250)$ , which are the number of subprojects that each student needs to complete for their project.

This is followed by  $d_i$  lines for each student i in the class, one line for each subproject in the order they must be completed by that student. Each line for a subproject consists of an integer t ( $1 \le t \le 1\,000\,000$ ), which is the amount of time it takes to complete the subproject, an integer p ( $1 \le p \le 1\,000\,000$ ), which is the priority of the subproject, and between zero and three distinct strings. Each of these strings will be one of Camera, Camcorder or Computer.

All priorities will be distinct.

### Output

For each student, display the time that they finish their last subproject, in the same order that the students are given in the input.





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| Sample Input 1 | Sample Output 1 |
|----------------|-----------------|
| 3              | 4 4 4           |
| 1 1 1          |                 |
| 1 1 1          |                 |
| 4 1 Camera     |                 |
| 4 2 Camcorder  |                 |
| 4 3 Computer   |                 |

| Sample Input 2      | Sample Output 2 |  |  |  |  |
|---------------------|-----------------|--|--|--|--|
| 3                   | 3 7 12          |  |  |  |  |
| 1 1 1               |                 |  |  |  |  |
| 1 1 1               |                 |  |  |  |  |
| 3 3 Computer        |                 |  |  |  |  |
| 4 2 Computer        |                 |  |  |  |  |
| 5 1 Camera Computer |                 |  |  |  |  |

| Sample Input 3 | Sample Output 3 |
|----------------|-----------------|
| 2              | 3 1             |
| 1 1 1          |                 |
| 2 1            |                 |
| 1 1 Computer   |                 |
| 1 3 Computer   |                 |
| 1 2 Computer   |                 |

| Sample Input 4                | Sample Output 4 |  |  |  |
|-------------------------------|-----------------|--|--|--|
| 3                             | 8 3 3           |  |  |  |
| 2 2 2                         |                 |  |  |  |
| 2 1 3                         |                 |  |  |  |
| 2 3 Camera                    |                 |  |  |  |
| 5 1 Camera Camcorder          |                 |  |  |  |
| 3 2 Camcorder Computer        |                 |  |  |  |
| 1 6 Camera Camcorder Computer |                 |  |  |  |
| 1 5 Camera Camcorder Computer |                 |  |  |  |
| 1 4 Camera Camcorder Computer |                 |  |  |  |



## Problem H Hilbert's Hash Browns Time limit: 1 second

You may have heard of Hilbert's Hotel. It has infinitely many rooms, and can cater for infinitely many guests. Each room has a number so even if it seems full, room for an extra guest can be found by asking every guest to move from room i to room i + 1, thus freeing up room 0. Unfortunately, the restaurant attached to the hotel, Hilbert's Hash Browns, is not infinite, although the number of tables is very large.



Source: xkcd.com, number 421, titled "Making Hash Browns"

To make matters worse, the waiter is very lazy. Rather than keep a record of which tables are available, he just assigns people to a table using a simple formula: when someone arrives at the restaurant, the waiter asks them their hotel room number. He raises this number to the power of p, and adds q. Since this gives very big numbers and there are only n tables (numbered 0 to n - 1), the waiter takes the remainder when dividing by n, and directs the customer to that table. Of course, sometimes the table is already occupied, in which case the customer goes away hungry.

The waiter uses a different value for p and q every day and he has noticed that some days a table never gets used no matter how many patrons turn up. For example if n = 3, p = 2 and q = 1, then table number 0 will never be used because there is no number x such that  $x^2 + 1 \equiv 0 \mod 3$ .

The waiter is lazy but he would like to appear competent. Can you help him determine the maximum number of tables that can be assigned for given values of p, q and n?

## Input

The input consists of a single line containing three integers p ( $1 \le p < 2^{31}$ ), q ( $0 \le q < 2^{31}$ ) and n ( $2 \le n < 2^{31}$ ).

## Output

Display the maximum number of tables that could be used.

| Sample Input 1 | Sample Output 1 |  |  |  |  |
|----------------|-----------------|--|--|--|--|
| 2 3 5          | 3               |  |  |  |  |
|                |                 |  |  |  |  |
| Sample Input 2 | Sample Output 2 |  |  |  |  |

This page is intentionally left (almost) blank.



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## Problem I Intuidiff II Time limit: 1 second

You may recall *Intuidiff*, the alternative to diff that we asked you to help develop at the Divisionals contest. Intuidiff gives an intuitive way to track changes in two files: the original document and the modified document.

We are now onto the next stage of development of Intuidiff. After some preprocessing, the original document has been broken up into several non-overlapping substrings, and each of these has been assigned a different colour (for example, see the 'Before' paragraph in Figure I.1). Then, in the modified document, the substrings are coloured using the same colours as those in the original document (for example, see the 'After' paragraph in Figure I.1). This allows us to see how large substrings have moved in the document. Substrings with the same colour may appear multiple times in the 'After' section, but only once in the 'Before' section. For example, the substring "et dolore magna aliqua." appears twice in the modified document of Figure I.1.

| Before                                       | After  |  |  |  |  |  |  |
|--|--|--|--|--|--|--|--|
| Lorem ipsum dolor sit amet, consectetur      | Lorem ipsum dolor sit amet, et dolore            |  |  |  |  |  |  |
| adipiscing elit, sed do eiusmod tempor       | magna aliqua. sed do eiusmod tempor              |  |  |  |  |  |  |
| incididunt ut labore et dolore magna         | incididunt ut labore consectetur adipiscing      |  |  |  |  |  |  |
| aliqua. Ut enim ad minim veniam, quis        | elit, quis nostrud exercitation Ut enim ad       |  |  |  |  |  |  |
| nostrud exercitation ullamco laboris nisi ut | minim veniam, ullamco laboris nisi ut            |  |  |  |  |  |  |
| aliquip ex ea commodo consequat.             | aliquip ex ea commodo consequat. <mark>et</mark> |  |  |  |  |  |  |
|  | dolore magna aligua.                             |  |  |  |  |  |  |

Figure I.1: A full colouring from the Intuidiff program.

While pretty, this full colouring might be overwhelming for some users. Also, it is distracting if every character is highlighted in the modified document. Attention should be focused only on the changes.

Therefore, for the next stage of development of Intuidiff, we must select which substrings to highlight. A full colouring of the document has already been decided on. We must select substrings from the full colouring in such a way that the non-highlighted characters are in the same order as in the original document.

The characters that are *not* highlighted must be in the same order as in the original document. The selection of substrings is done in such a way that the number of non-highlighted characters in the modified document is maximised (for example, see Figure I.2).

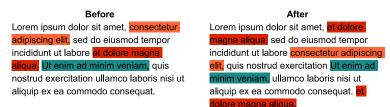


Figure I.2: A desired colouring from the Intuidiff program.

### Input

The first line of input contains a single integer n ( $1 \le n \le 100000$ ), which is the number of coloured substrings in the full colouring in the modified document. The next n lines describe the coloured substrings in the modified document. Each of these lines contain two integers a and b ( $0 \le a \le b \le 10^9$ ), which is the substring of the original document running from the character at index a to the character at index b, inclusive.

No two substrings will partially overlap. That is, if two substrings share any common indices, then the substrings will be identical.





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## Output

Display the number of characters that are not highlighted by Intuidiff in the modified document.

## Notes

Sample Input 1 is the 'After' paragraph from Figure I.1. The 154 non-highlighted characters are shown in Figure I.2.

| Sample Input 1 | Sample Output 1 |
|----------------|-----------------|
| 8              | 154             |
| 0 27           |                 |
| 99 122         |                 |
| 56 98          |                 |
| 28 55          |                 |
| 148 174        |                 |
| 123 147        |                 |
| 175 230        |                 |
| 99 122         |                 |

| Sample Input 2 | Sample Output 2 |
|----------------|-----------------|
| 5              | 6               |
| 1 1            |                 |
| 10 11          |                 |
| 5 7            |                 |
| 3 4            |                 |
| 10 11          |                 |



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## Problem J **Just Terraffic!** Time limit: 1 second

The local council is recording traffic flow using a pressure pad laid across the road. The pressure pad tracks whenever the wheels on an axle of a vehicle cross the pressure pad. The only vehicles using the road are cars with two axles. Each vehicle may or may not have a single-axle trailer attached to it. When a car crosses the pressure pad, two times are recorded: one when the front wheels cross and another when the rear wheels cross. If the car is towing a trailer an additional time is recorded when the trailer wheels cross. Given a sequence of times from the recorder, the council wishes to know how many cars without trailers crossed the pad and how many cars with trailers crossed it.



Obviously, there is some ambiguity. For example, a sequence of 6 recordings could be three cars without trailers or two cars with trailers. To reduce such ambiguity, we will make the following two assumptions:

- 1. Any two successive times with a difference less than or equal to 1000 ms must belong to the same vehicle.
- 2. Any two successive times with a difference greater than or equal to 2000 ms must be from different vehicles.

Given a sequence of times, determine the number of cars with and without a trailer.

### Input

The first line of the input contains a single integer n ( $1 \le n \le 300\,000$ ), which is the number of times the pressure pad was triggered. The second line contains n distinct integers  $t_1, \ldots, t_n$   $(0 \le t_i < 2^{30})$  in increasing order, the times that the pressure pad was triggered. The times are in milliseconds.

## Output

Display the number of cars with and without trailers. If the number of cars of each type can be uniquely determined, then display two lines of the form

```
Cars without trailers: X
Cars with trailers: Y
```

If there is no interpretation of the times that is consistent with the assumptions, then display Impossible. If there are multiple interpretations of the times that give different numbers of cars with and without trailers, then display Ambiguous.

| Sample Input 1                  | Sample Output 1          |  |  |  |  |
|---------------------------------|--------------------------|--|--|--|--|
| 7                               | Cars without trailers: 2 |  |  |  |  |
| 10 200 5000 6100 7200 8300 9400 | Cars with trailers: 1    |  |  |  |  |

#### Sample Input 2

| Sample Output 2 |
|-----------------|
| Ambiguous       |
|                 |
|                 |
| Sample Output 3 |
|                 |

| 4                | Impossible |
|------------------|------------|
| 0 1000 2000 3001 |            |

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## Problem K Kiwis vs Kangaroos Time limit: 1 second

As everyone in this room knows, there is an ongoing feud between the national animals of Australia and New Zealand: the kangaroos and the kiwis! Centuries ago, kangaroos and kiwis were great friends and played happily with one another all day and all night. Over time, they both became too tired to play 24 hours per day, so they had to decide what time of day they should play: the day time (preferred by the kangaroos) or the night time (preferred by the kiwis). This disagreement started the feud that has lasted ever since.

The king of the kangaroos and the queen of the kiwis are now at a secret meeting under the Tasman Sea in hopes of stopping this feud. After hours of negotiations,

they decide that the only fair way to settle the feud is to get a neutral third party to decide. And that third party is you! You have come up with the following algorithm to determine the winner:

- 1. The kangaroo king and kiwi queen must agree upon a secret phrase.
- 2. Each animal is given a key: KANGAROO for the kangaroos and KIWIBIRD for the kiwis.
- 3. For each letter in the secret phrase, count the number of times that letter appears in the animal's key. Uppercase and lowercase should be treated as the same.
- 4. The total score for each animal is the sum of these counts.
- 5. The animal with the higher total score is the winner.

For example, if the secret phrase is "Australia", then the kangaroos' score would be 7 and the kiwis' score would be 4. In this case, the kangaroos would win the feud.

|          | Α | u | S | t | r | а | 1 | i | а | Total |
|----------|---|---|---|---|---|---|---|---|---|-------|
| KANGAROO | 2 | 0 | 0 | 0 | 1 | 2 | 0 | 0 | 2 | 7     |
| KIWIBIRD | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 3 | 0 | 4     |

Given the secret phrase, who wins the feud?

### Input

The input will consist of text on one line, the secret phrase. The secret phrase will be non-empty and contain only uppercase letters and lowercase letters. The secret phrase will contain at most 100 characters.

## Output

If there is a winner of the feud, display the winner's name: either Kangaroos or Kiwis. If there is a tie, display Feud continues instead.

| Sample Input 1      | Sample Output 1 |
|---------------------|-----------------|
| BattlestarGalactica | Kangaroos       |
| Sample Input 2      | Sample Output 2 |
| RiddlesInTheDark    | Kiwis           |
| Sample Input 3      | Sample Output 3 |
| Hexadecimal         | Feud continues  |



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